

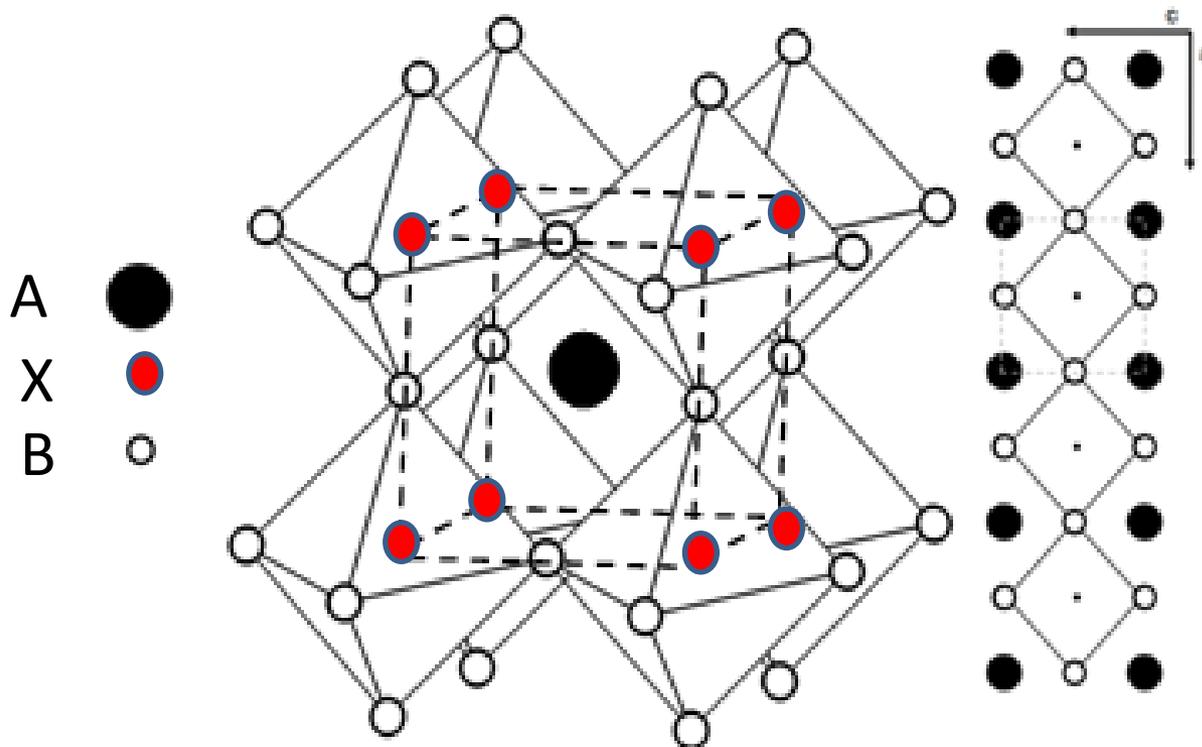
Hybrid Perovskite Solar Cells

Annamaria Petrozza

"ORGANIC ELECTRONICS : principles, devices and applications"

Milan, Novembre 27th, 2015

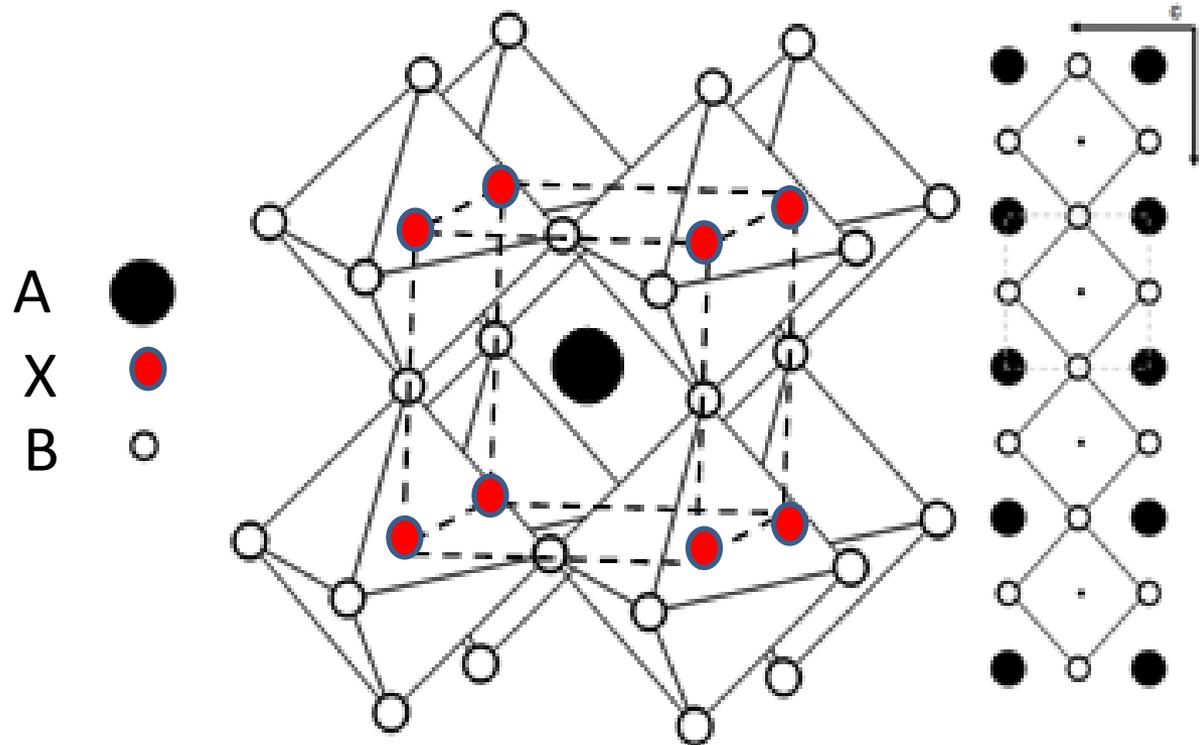
Perovskite Crystal with ABX_3 stoichiometry



**I-V-O₃, II-IV-O₃
 and III-III-O₃ e.g.
 KTaO₃, SrTiO₃
 and GdFeO₃**

**I-II-X₃, e.g.
 CsSnI₃,
 CH₃NH₃PbI₃,**

It is not only a matter of stoichiometry....

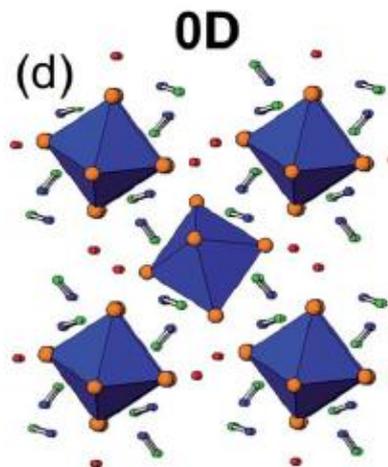
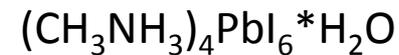
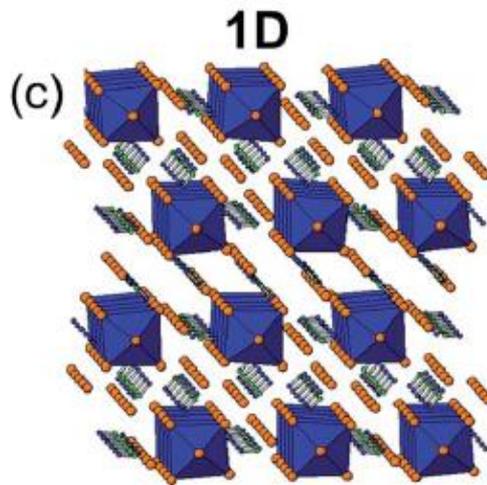
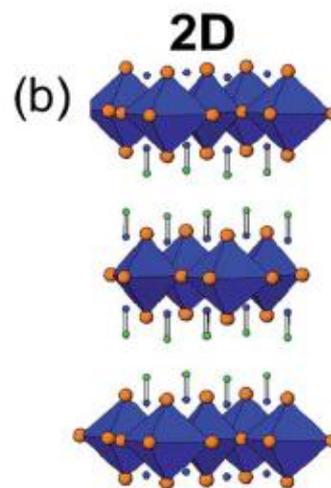
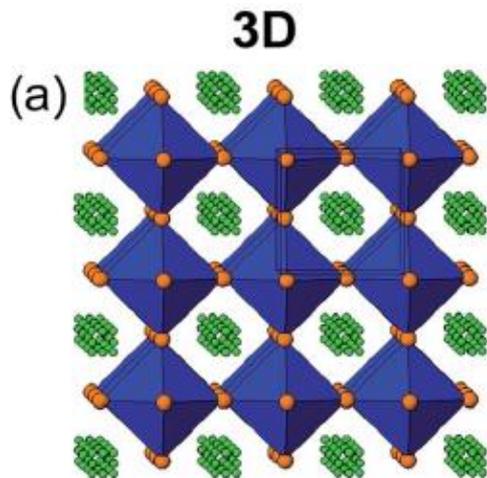


The Goldschmidt tolerance factor:

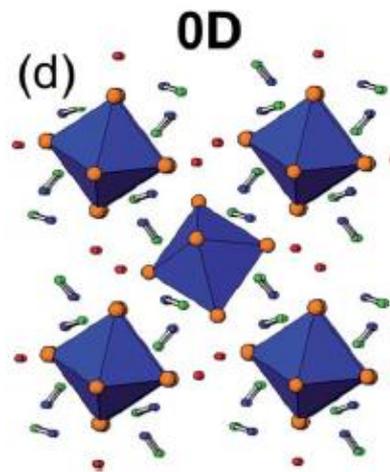
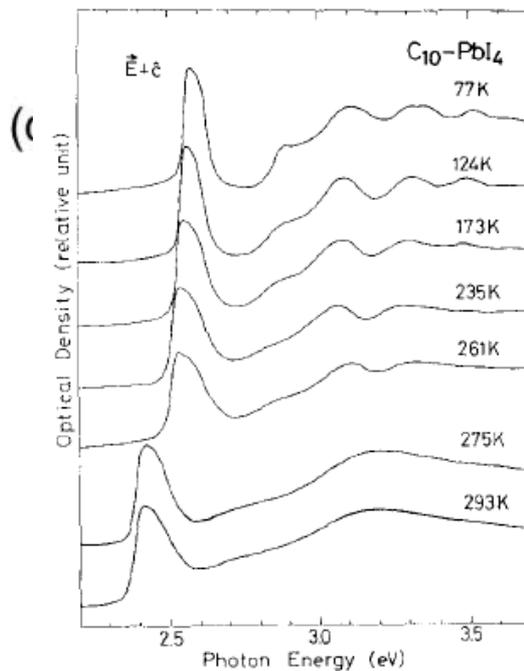
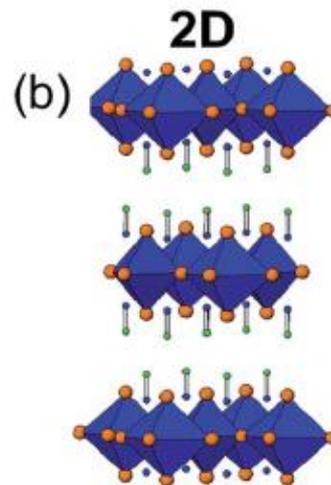
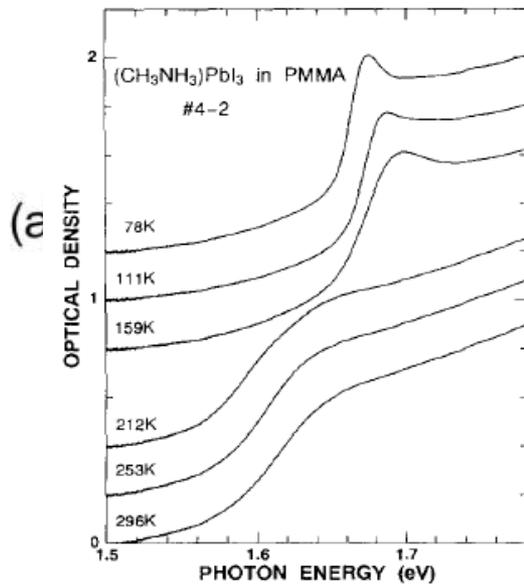
$$t = \frac{R_A + R_X}{\sqrt{2}(R_B + R_X)}$$

$t < 0.7$ the perovskite falls apart
 $t > 1$ towards 2D structures...

Playing with Dimensionality

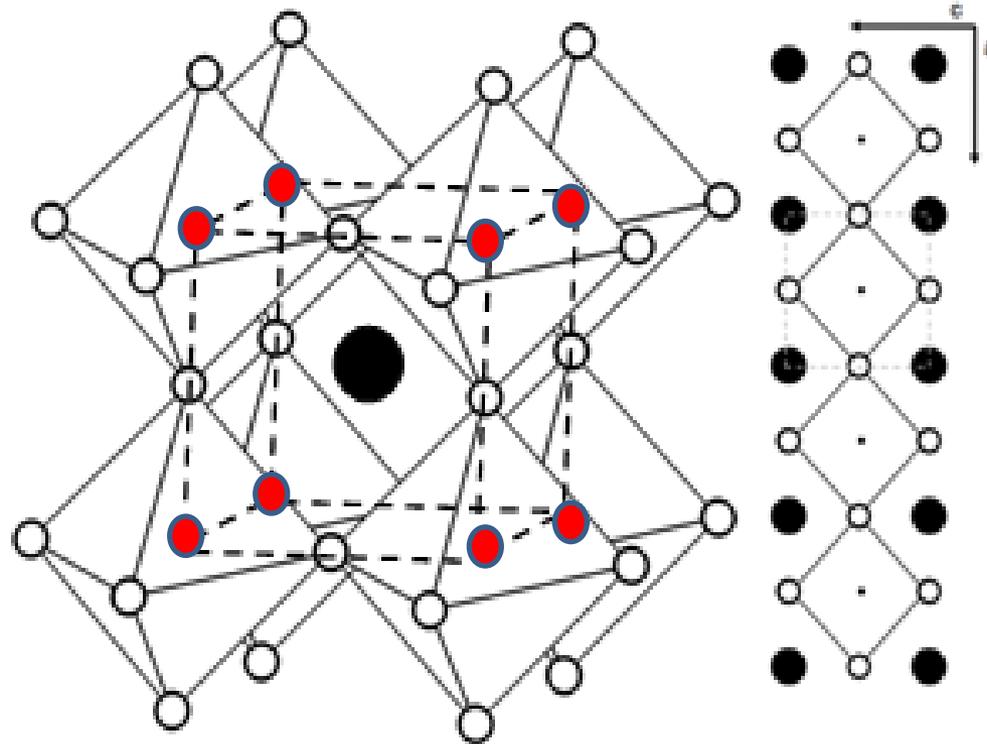


Dielectric Confinement

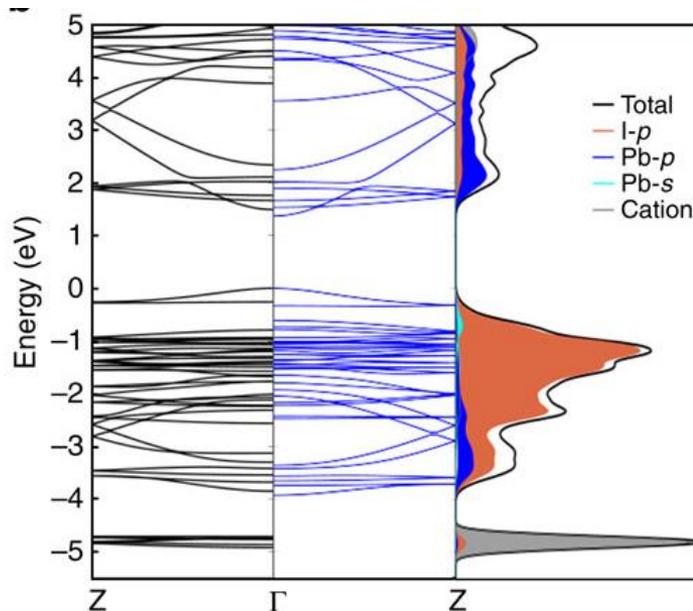
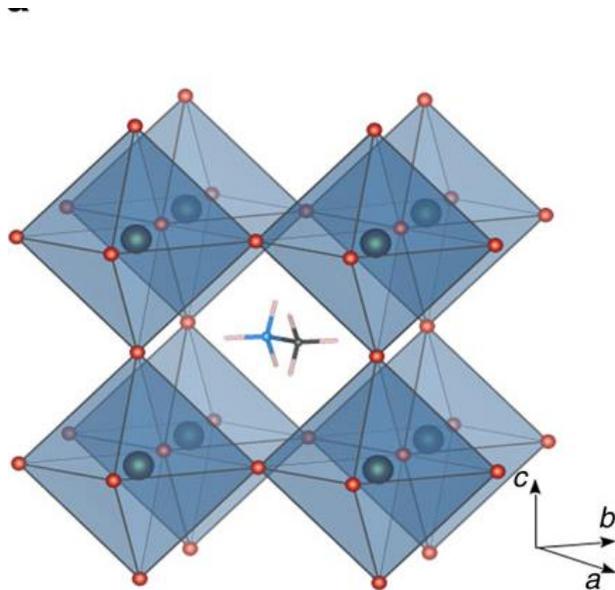


Ishihara, J. Lum, 1994.

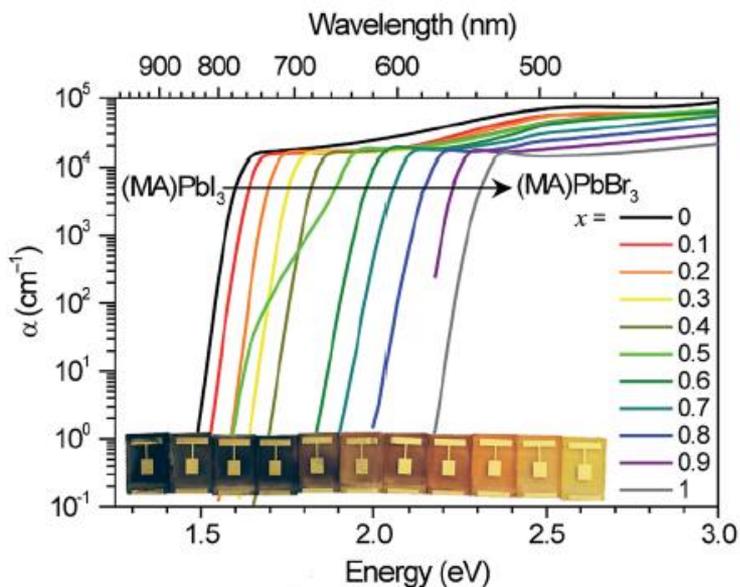
Organo-Metal Halide Crystalline Perovskite



Organo-Metal Halide Crystalline Perovskite

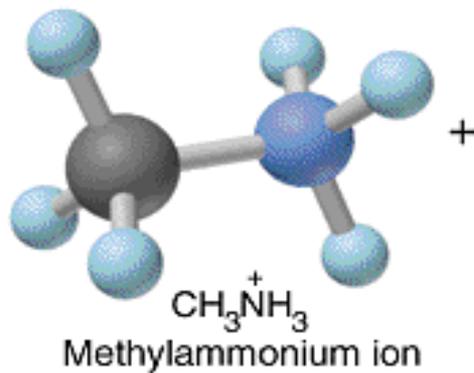


Filip et al, Nat Comm, 2014



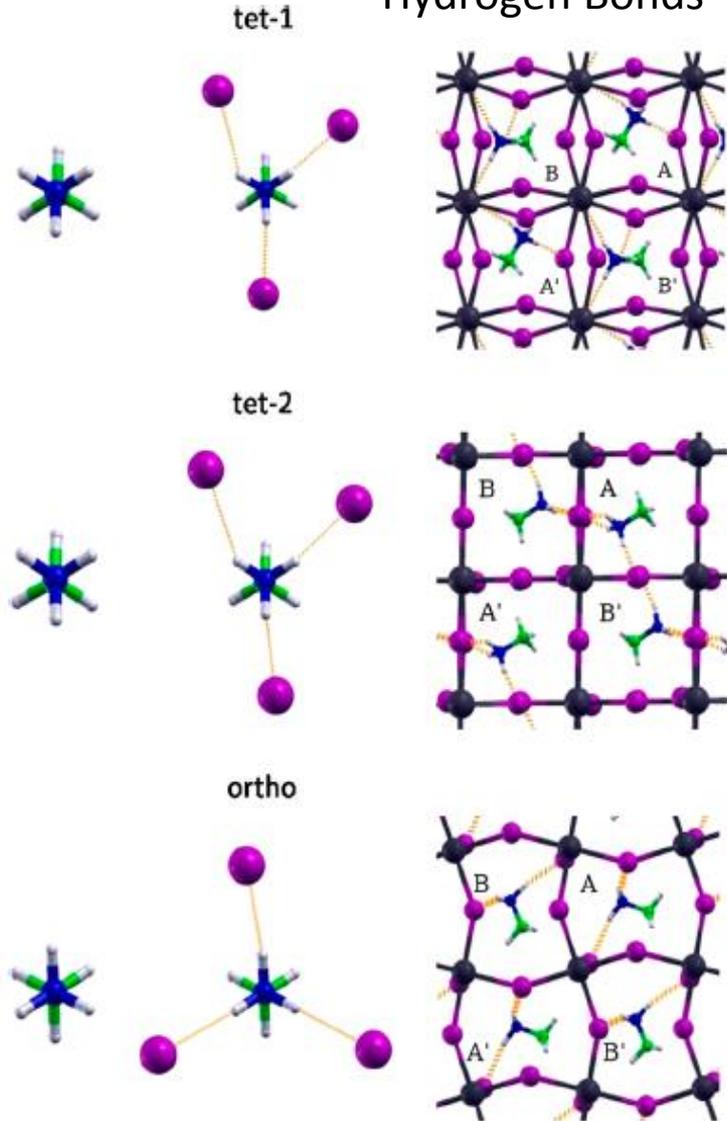
Eric Hoke et al, Chem Sci, 2015

Organo-Metal Halide Crystalline Perovskite

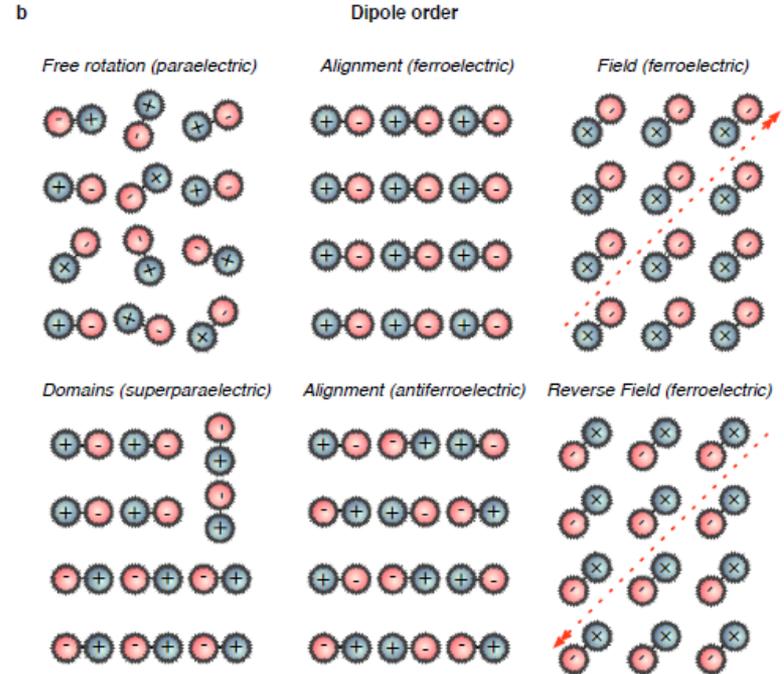
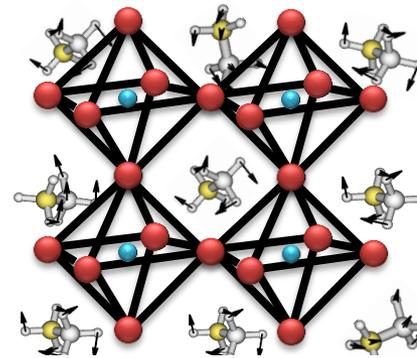


CH_{3NH₃⁺ :Orientational disorder and Polarizability}

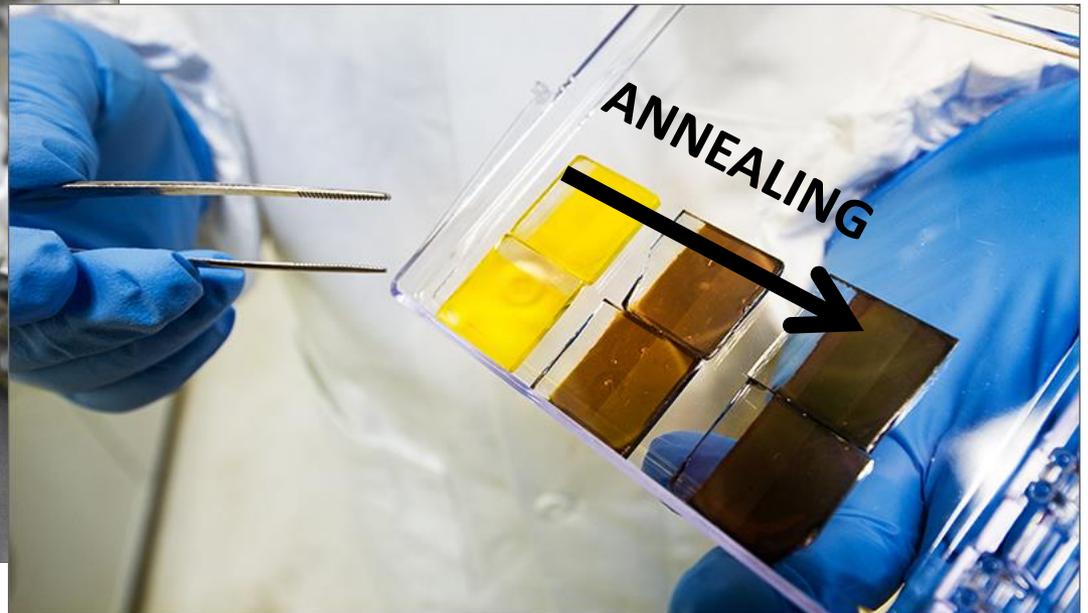
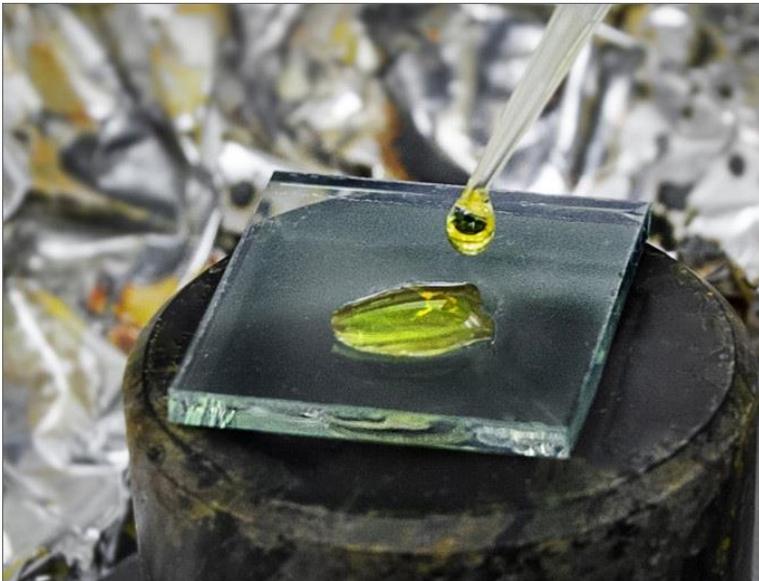
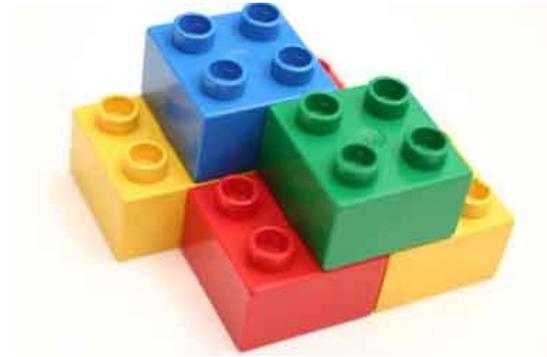
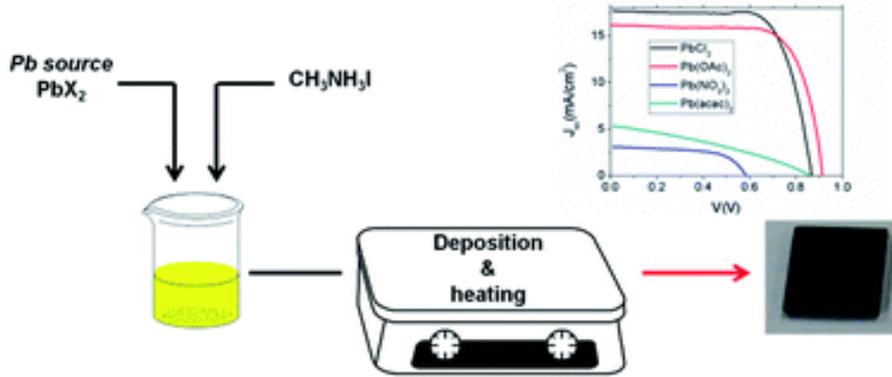
Hydrogen Bonds



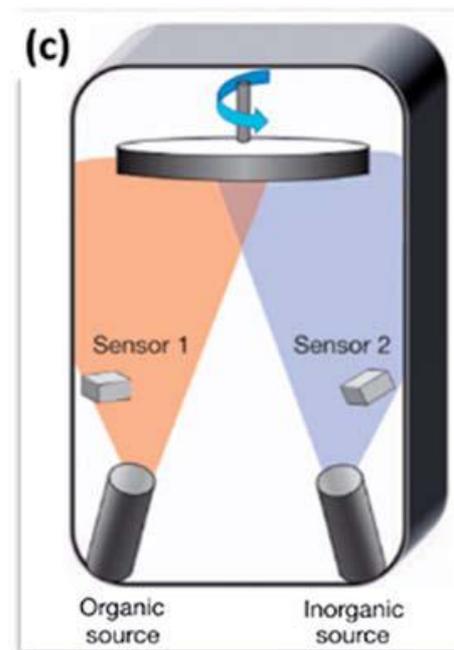
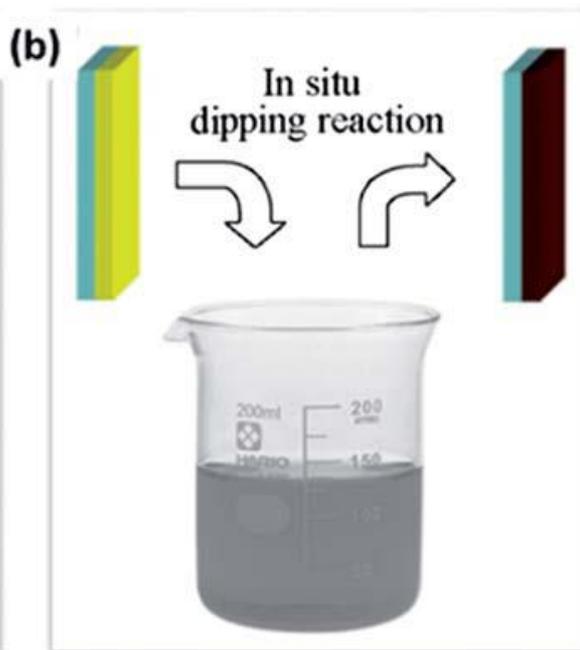
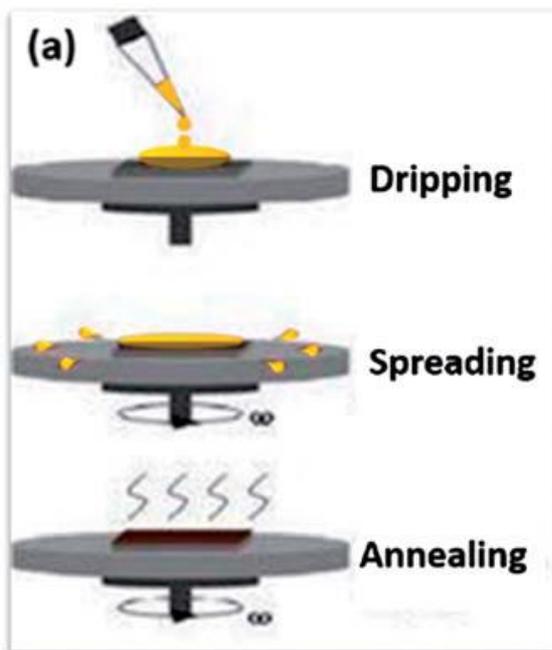
Dipole "nearly" free to move



Modular Structure

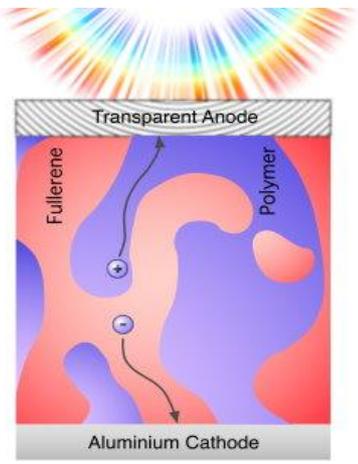


Prone to a variety of processing methods

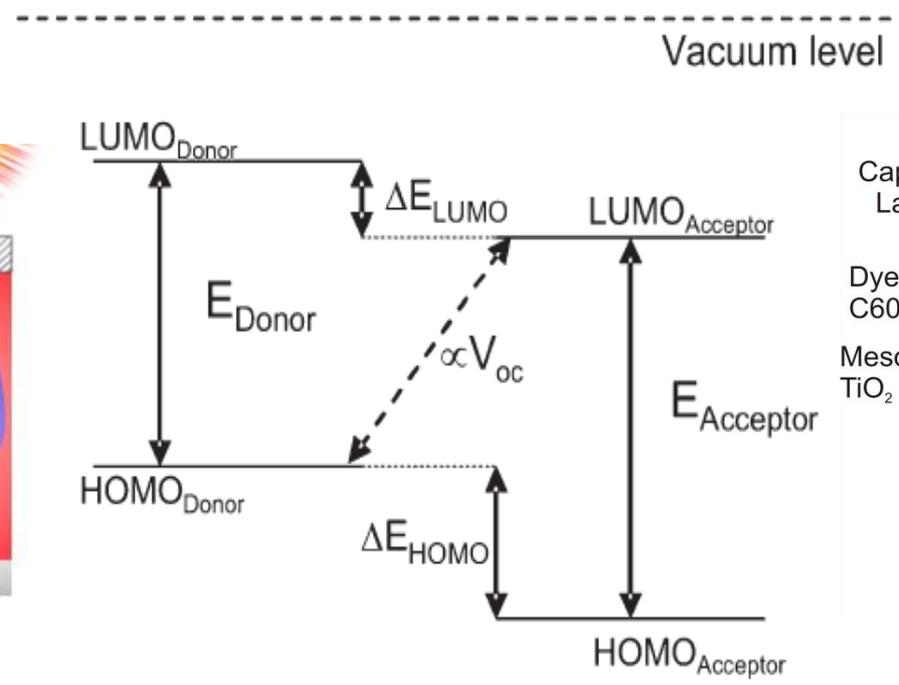
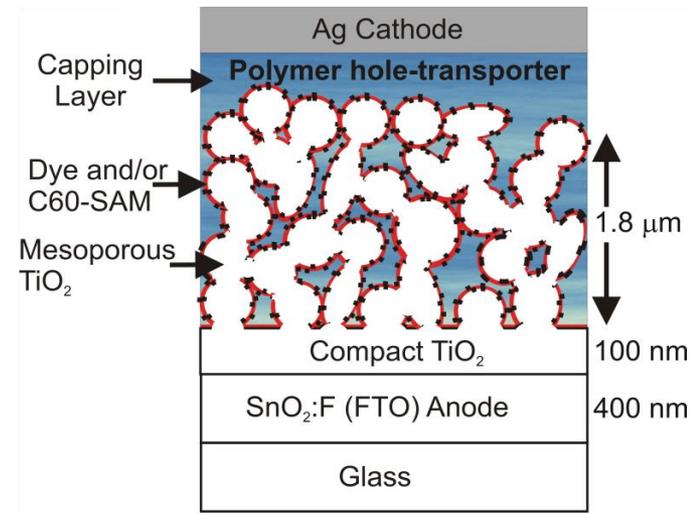


Excitonic Solar Cells

OPV

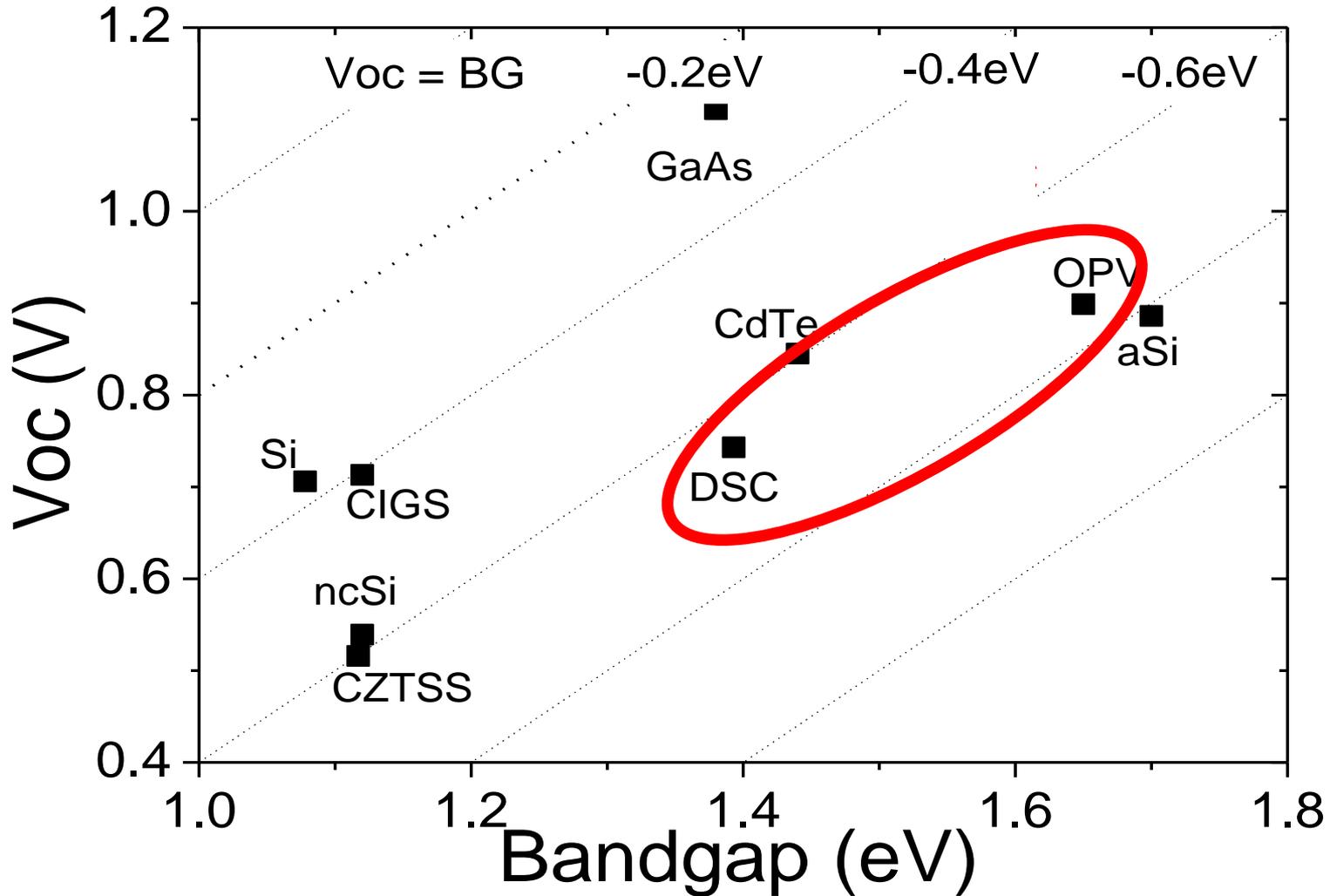


DSSC



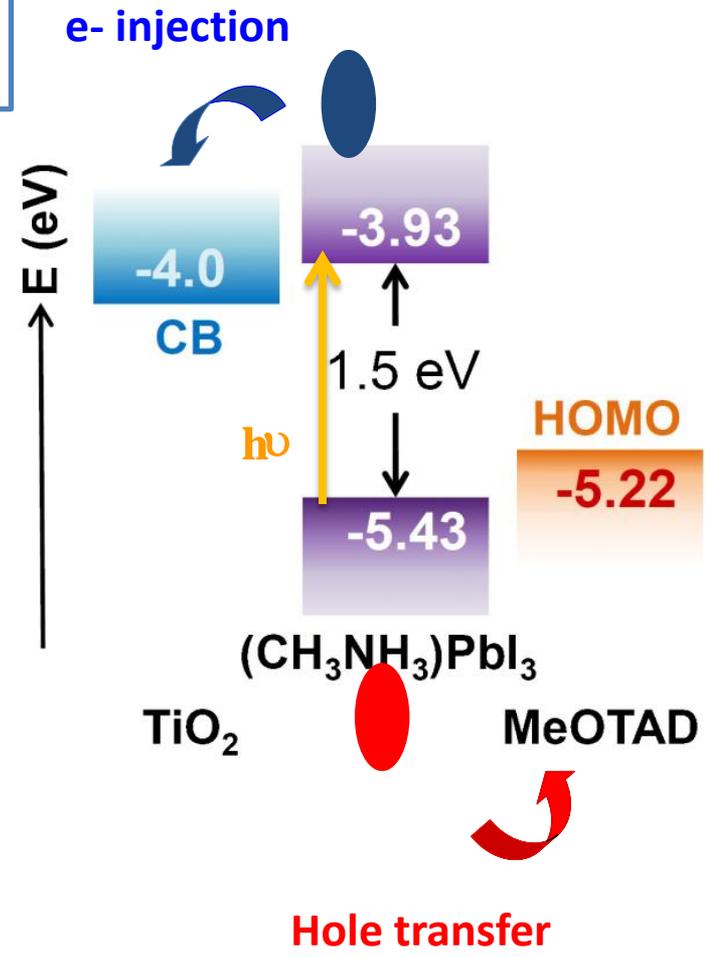
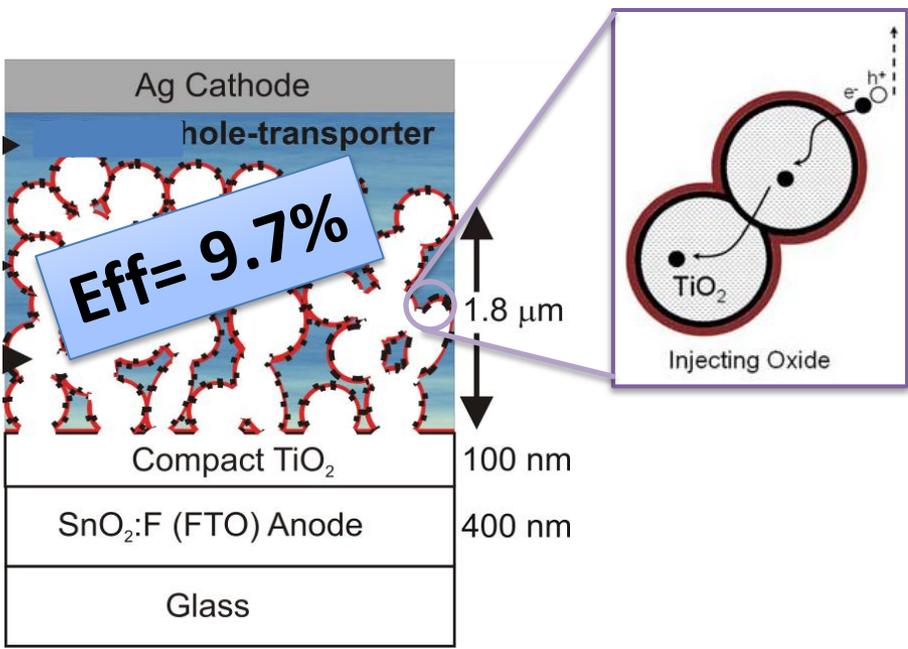
Type II Hetero-Junction

Intrinsic Loss in Excitonic Solar Cells

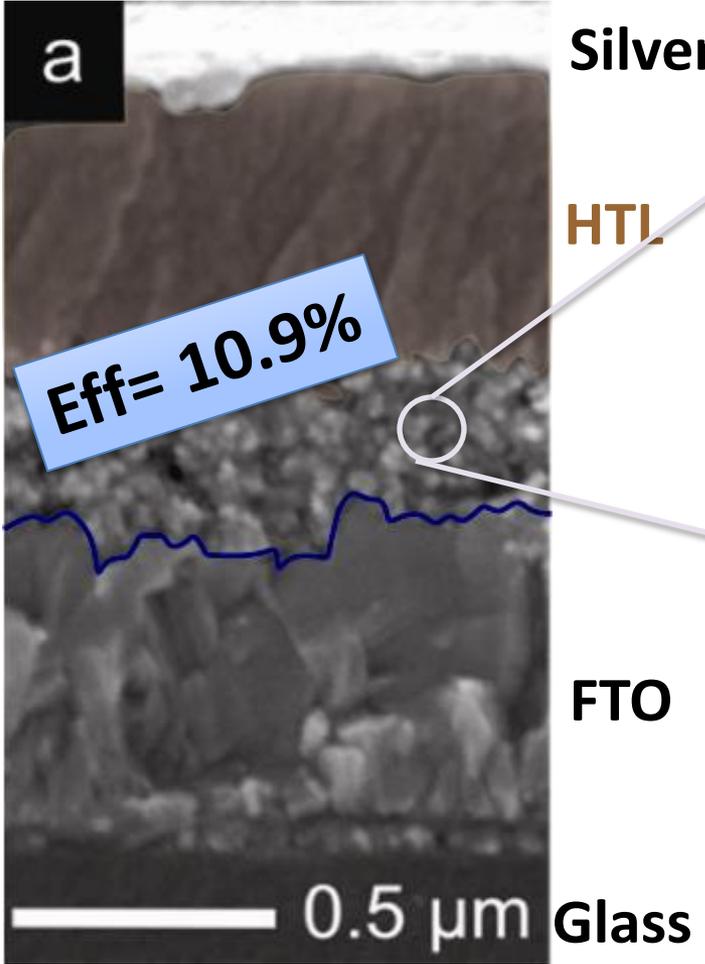


Hybrid Crystals in DSSC Devices

$\text{CH}_3\text{NH}_3\text{PbI}_3$ perovskite as light antenna in the **DSSC** concept



Hybrid Crystals in Hybrid Solar Cells

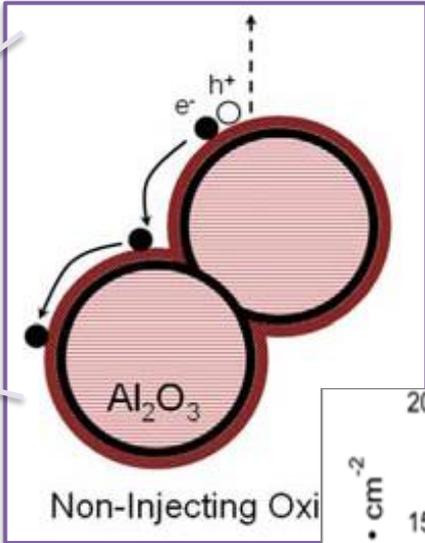


Silver

HTL

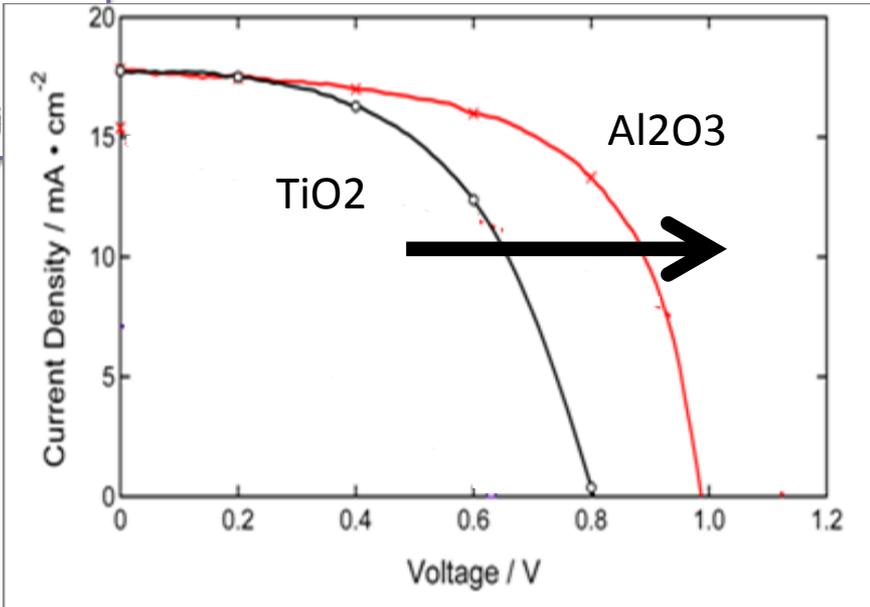
FTO

Glass



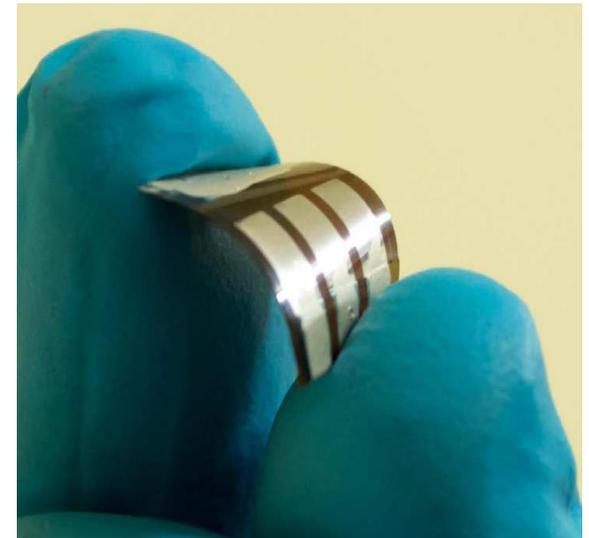
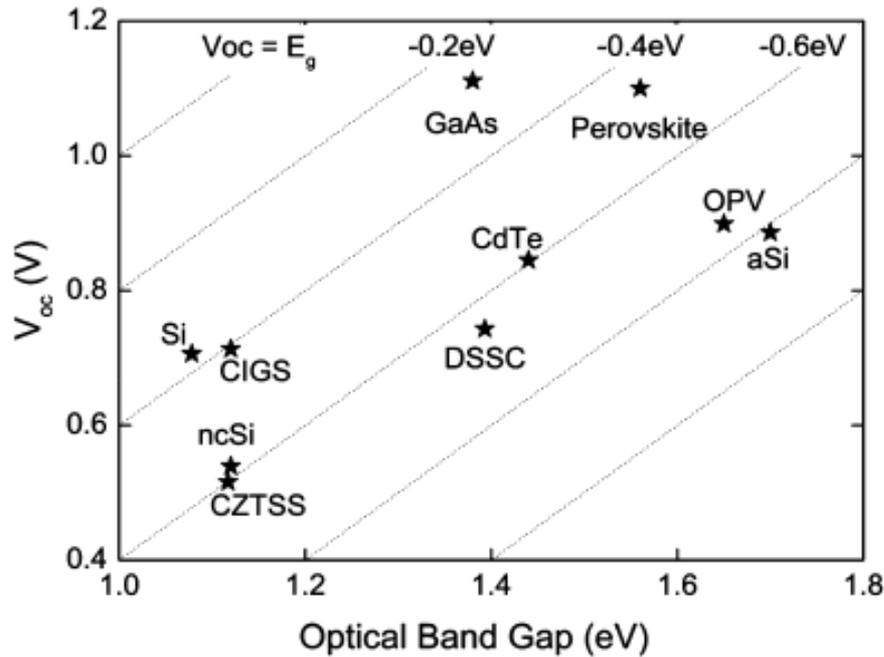
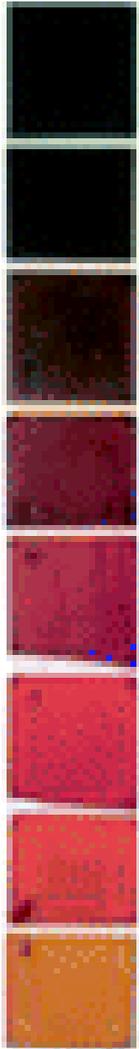
Perovskite role:

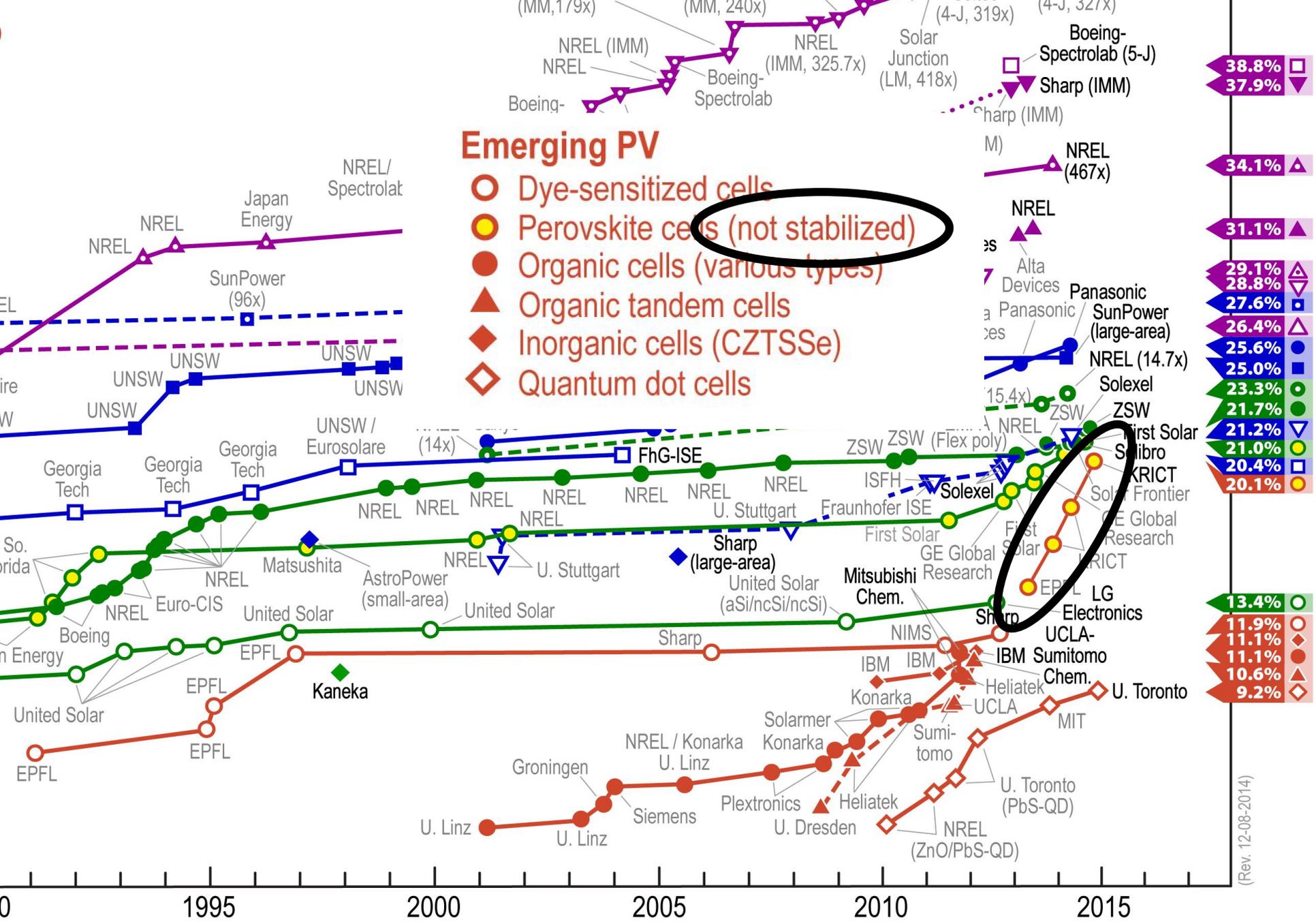
- Absorber
- Electron-transporter



M.Lee et al. *Science* 338, 643 (2012)

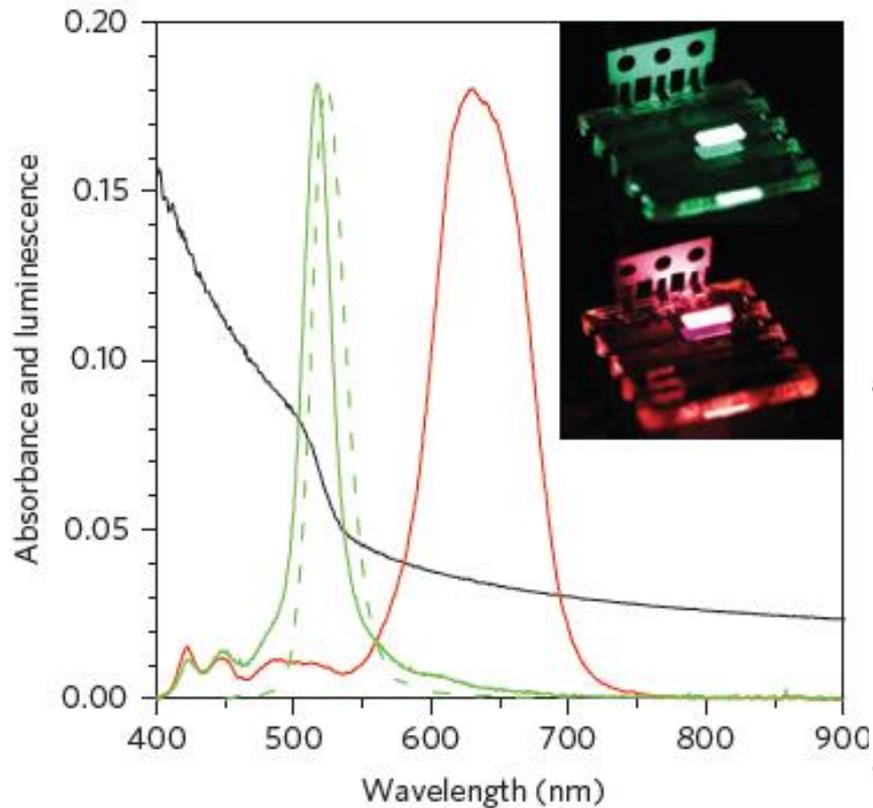
Which is their strength?





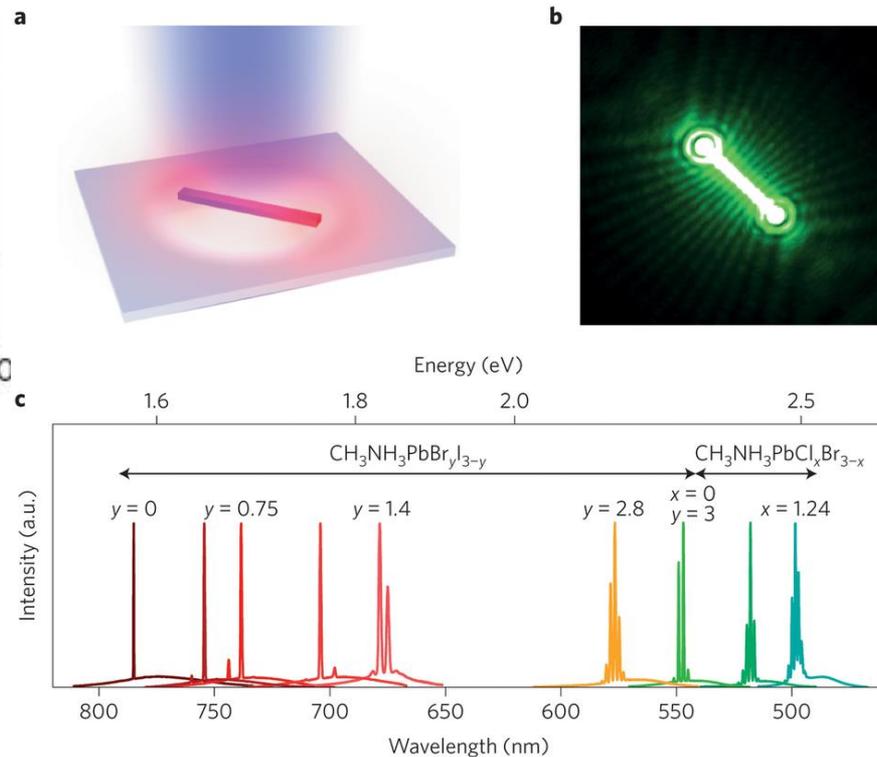
(Rev. 12-08-2014)

Optoelectronic Devices

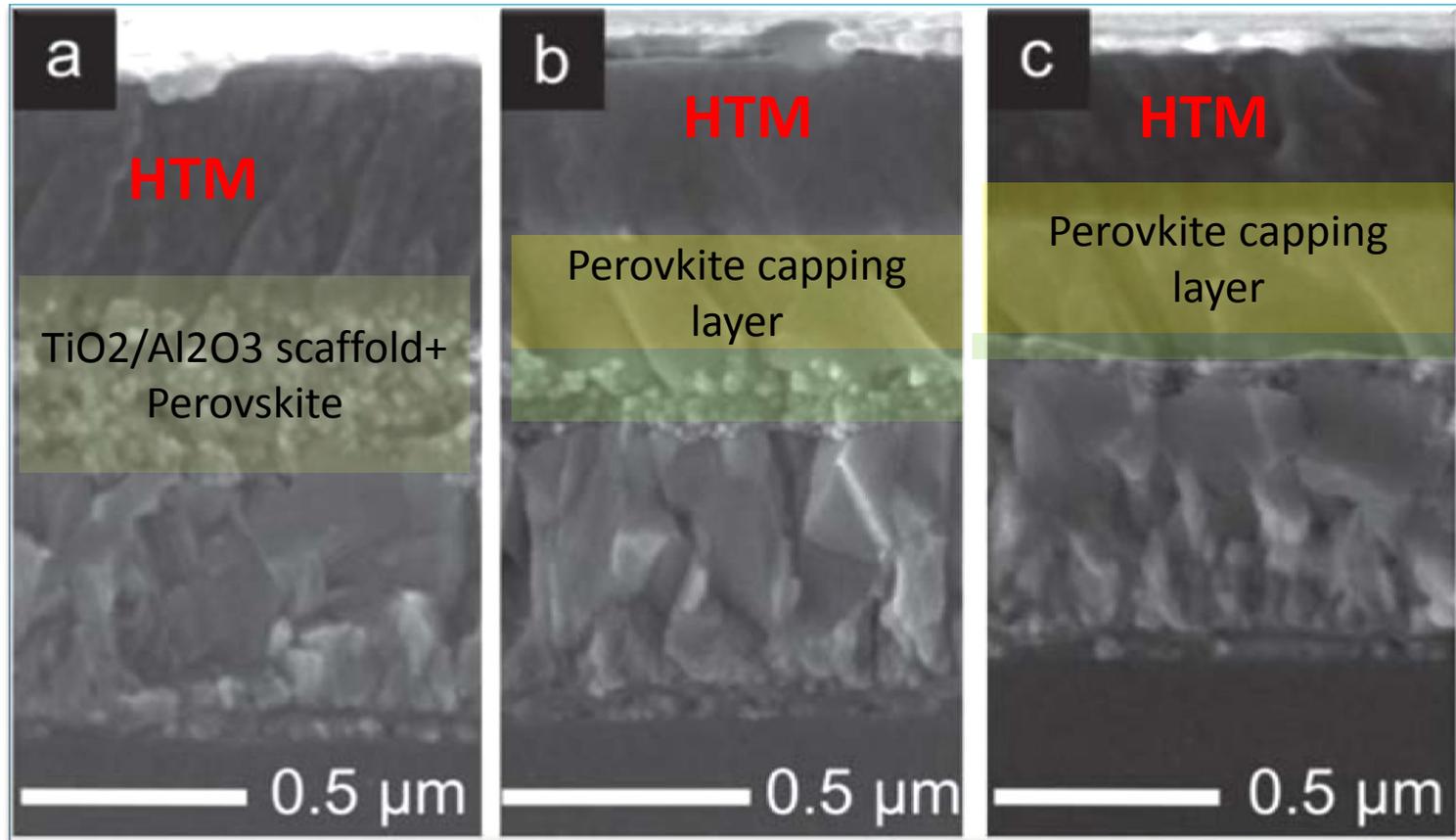


Tan et al, Nat Nanotech, 2014

Zhu et al, Nat Mat, 2015



Designing the Device Architecture



Nano-structured vs Thin Film

Designing the Device Architecture

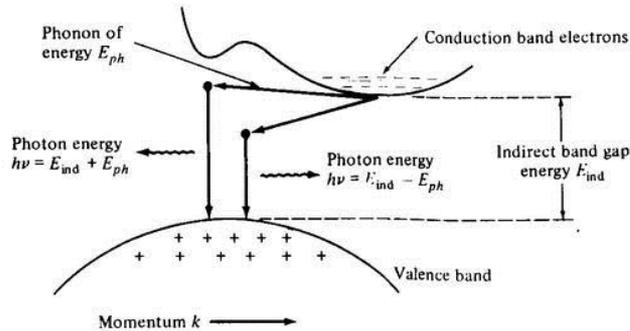
- Light Absorption
- Charge Generation
- Photo-carriers Transport

Designing the Device Architecture

- **Light Absorption**
- Charge Generation
- Photo-carriers Transport

Light Absorption

Silicon



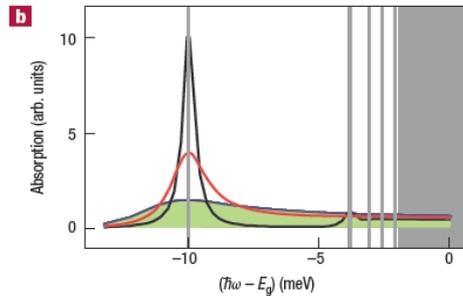
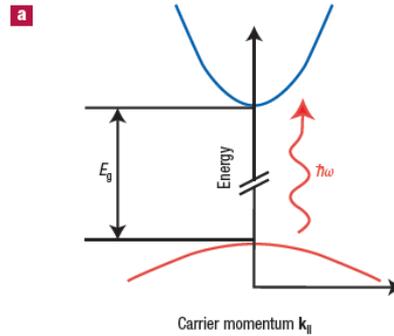
➤ In direct band-gap
Phonon assisted

➤ um range sun light
penetration depth

➤ thick solar cells

➤ no light emission

GaAs

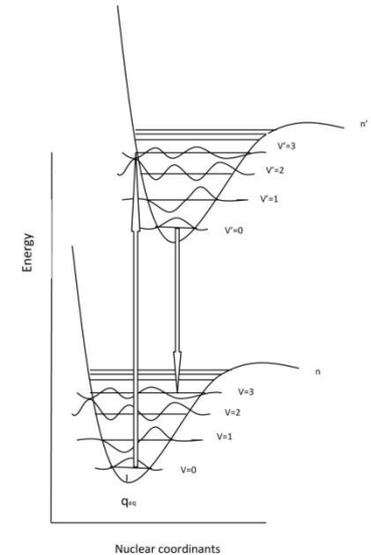


➤ direct band-gap

➤ excitonic effects at
absorption edge

➤ good light
penetration depth

Dyes/conjugated polymers



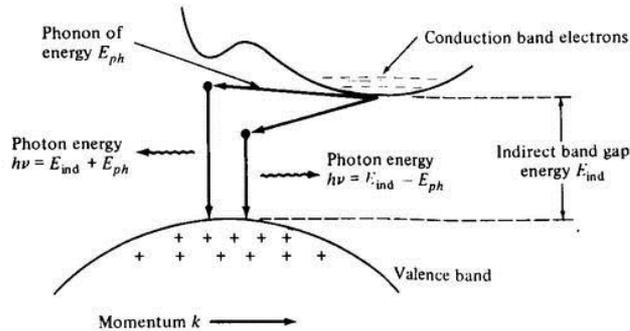
➤ localized states

➤ excitonic effects

➤ large absorption
cross-section/ efficient
carrier recombination

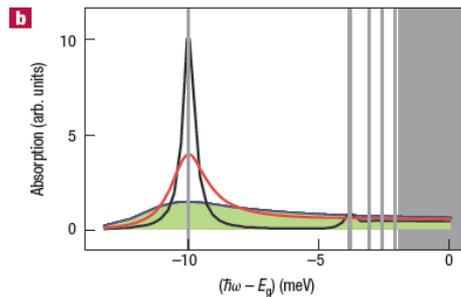
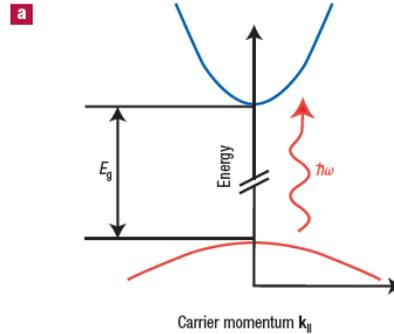
Light Absorption

Silicon



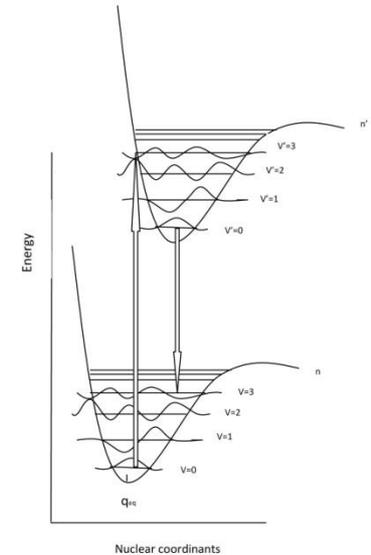
- In direct band-gap Phonon assisted
- μm range visible light penetration dept
- thick solar cells
- no light emission

GaAs



- direct band-gap
- excitonic effects at absorption edge
- good light penetration depth

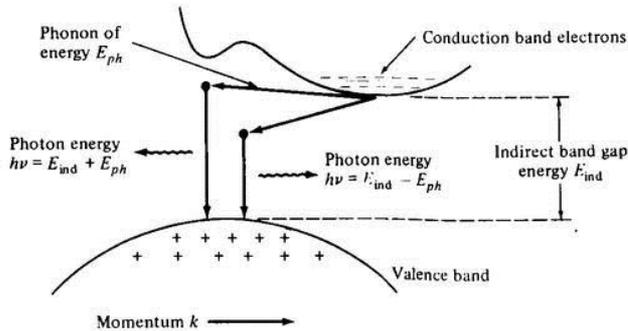
Dyes/conjugated polymers



- localized states
- excitonic effects
- large absorption cross-section/ efficient carrier recombination

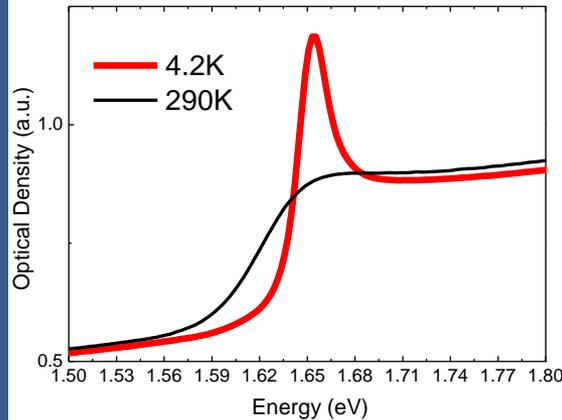
Light Absorption

Silicon



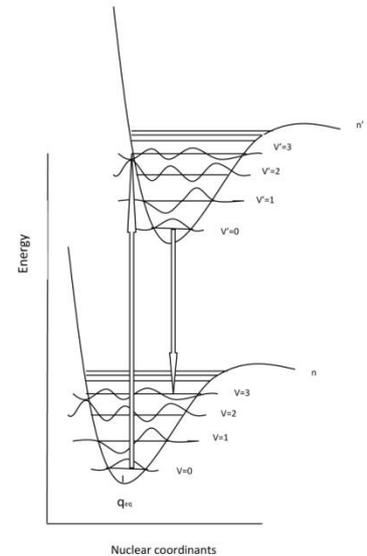
- In direct band-gap Phonon assisted
- μm range visible light penetration dept
- thick solar cells
- no light emission

Hybrid Perovskites



- direct band-gap
- excitonic effects at absorption edge
- good light penetration depth

Dyes/conjugated polymers



- localized states
- excitonic effects
- large absorption cross-section/ efficient carrier recombination

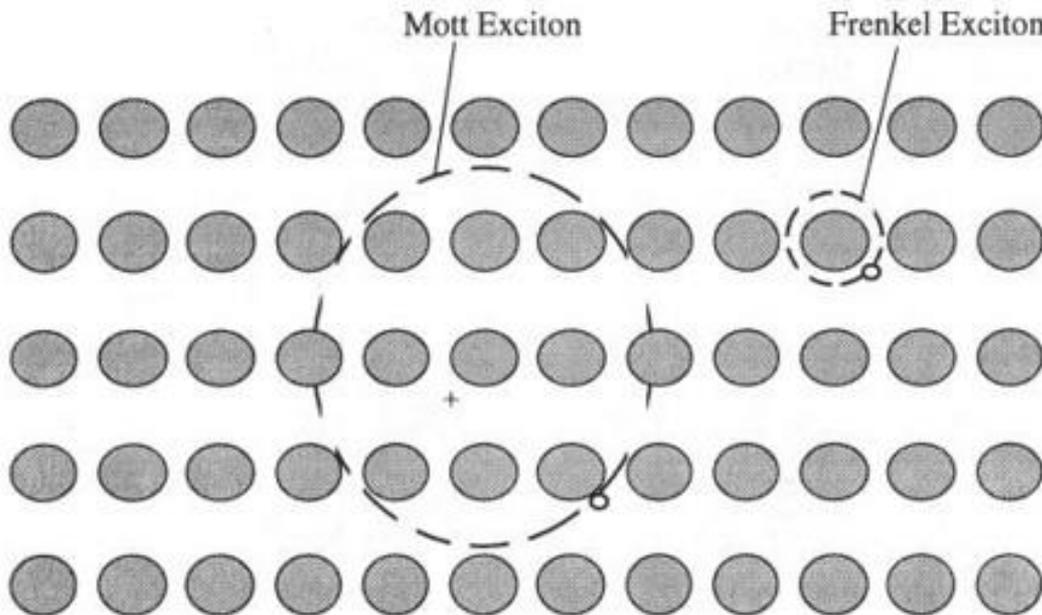


“ ..is a quasi-particle that represents a collective excited state of an ensemble of atoms or molecules. It is represented by a wavepacket for which we can define mass and speed which transports Energy”

How many kind of excitons??

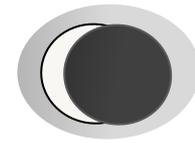
Wannier-Mott

Frenkel

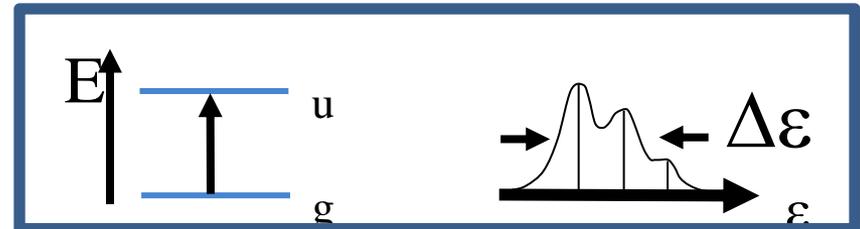


- Binding energy**
- Delocalization**
- Oscillator strength**
- Triplet**
- Singlet**
- Lifetime**

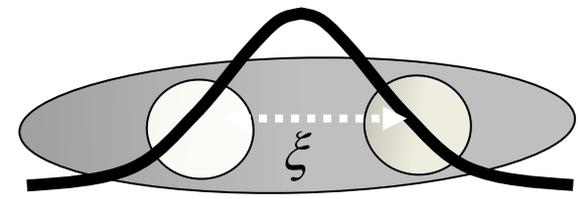
Frenkel Exciton



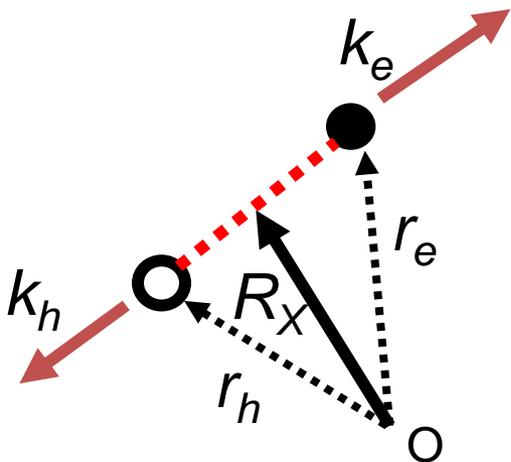
- Solids made by weakly interacting units (e.g organic crystals, inter-molecular coupling weaker than the intra-molecular ones).
- General case of a Molecular Excitation (**DSSC**)
- The wavefunction squared amplitude is the probability of finding the excited state in the lattice.



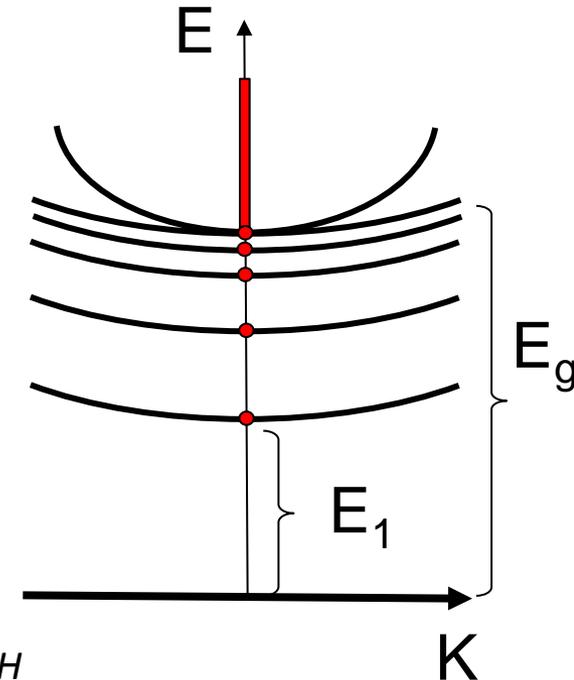
Wannier-Mott



- Solids with tightly bounded atoms
- Low Screening → Coulomb attraction does not allow the generation of FREE e-h pairs
- Hydrogenoid system.
- Center of Mass/Exciton radius (LARGER than the lattice constant)



$$E_{K_X, n} = E_g - \frac{E_b}{n^2} + \frac{\hbar^2 K_X^2}{(m_e^* + m_h^*)}$$

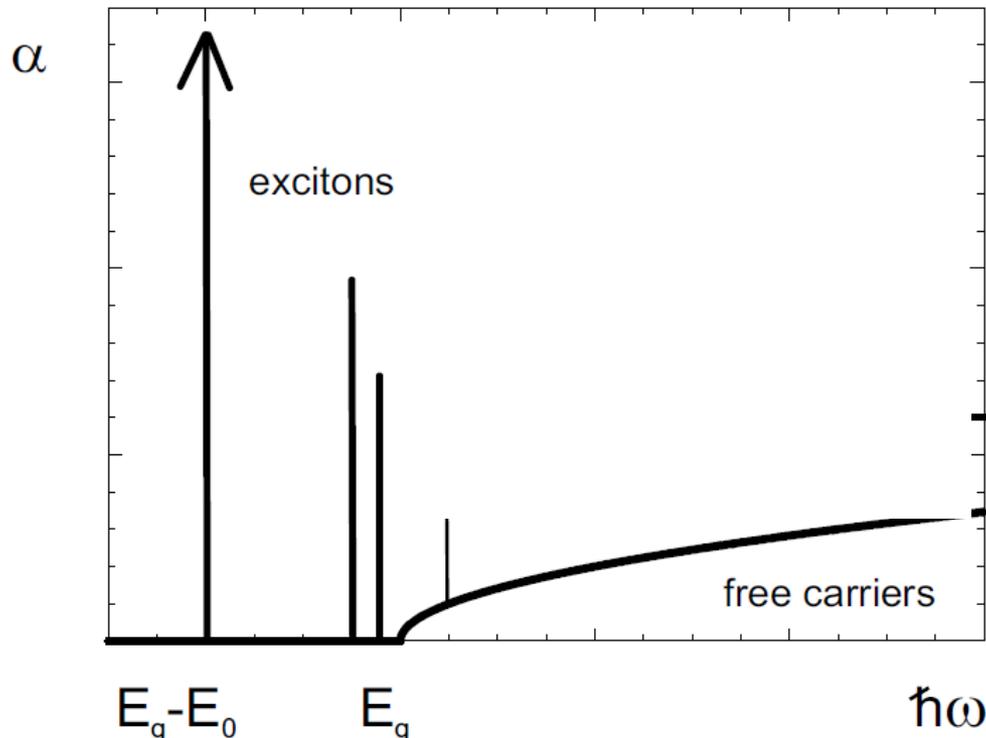


Why do we need to know the details?

- **Energy spent in the exciton dissociation**

Why do we need to know the details?

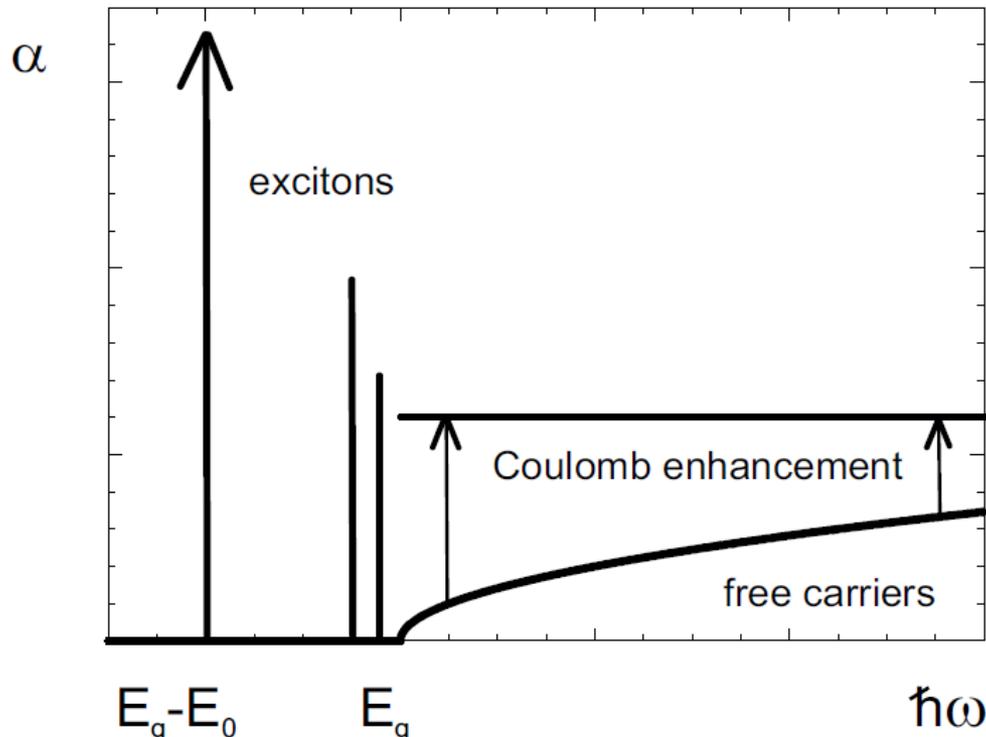
- Energy spent in the exciton dissociation
- Absorption cross section enhancement



$$\alpha_X \propto \frac{1}{\pi(a_B)^3}$$

Why do we need to know the details?

- Energy spent in the exciton dissociation
- Absorption cross section enhancement



$$\alpha_{cont} = \alpha_{free} C(\omega)$$

$$C(\omega) = \frac{\frac{\pi}{\sqrt{\Delta}} e^{\pi/\sqrt{\Delta}}}{\sinh(\pi/\sqrt{\Delta})}$$

$$\Delta = (\hbar\omega - E_g) / E_0$$

Elliott's Theory (1963)

Exciton Vs Free Charges

at the Thermodynamic Equilibrium

Total excitation density

Excitons

$$n = n_{FC} + n_{exc}$$

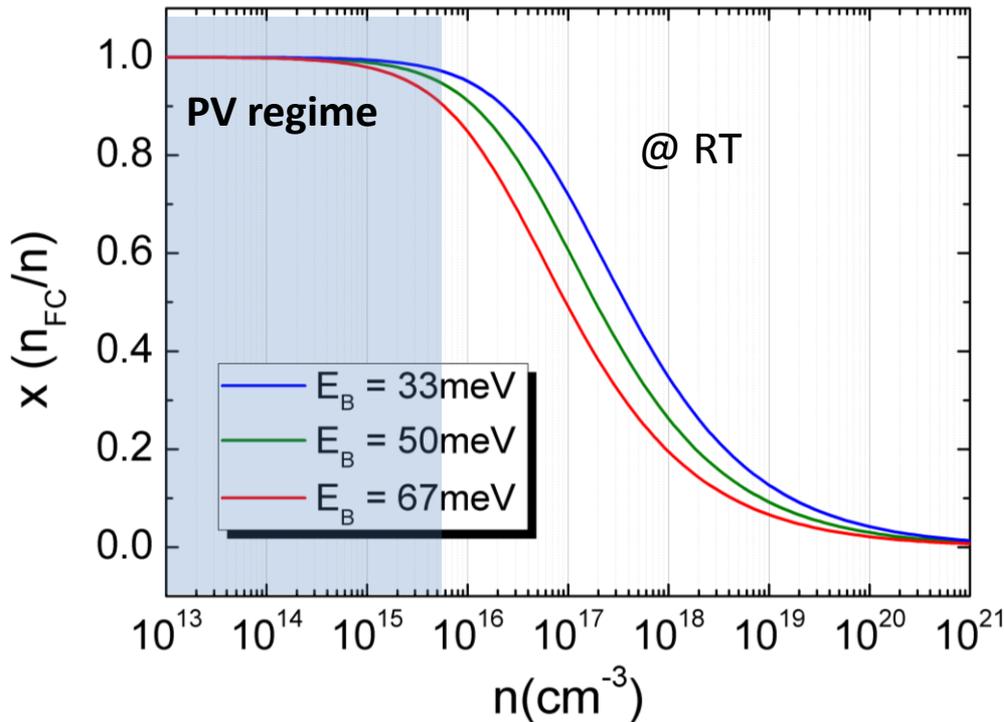
Free charges

Law of mass action

$$\frac{n_{FC}}{n_{exc}} = \left(\frac{2\pi\mu k_B T}{h^2} \right)^{3/2} e^{-\frac{E_b}{k_B T}}$$

Saha-Langmiur equation

$$x = \frac{n_{FC}}{n}$$



@ RT

Exciton Binding Energy

$$a_B = \frac{\hbar^2 \varepsilon}{\mu e^2}$$

Exciton Reduced mass

$$\mu = \frac{m_e m_h}{m_e + m_h}$$

$$E_B = \frac{\mu e^4}{2\hbar^2 \varepsilon^2} = \frac{\hbar^2}{2\mu a_B^2}$$

Dielectric constant

Bohr Radius

The golden rule:

“the Bohr orbital frequency (E_b/h) must be compared with the optical phonon frequency”

Dielectric constant (ϵ):

A measure of a substance's ability to insulate charges from each other.

Screening in solids: basic concept

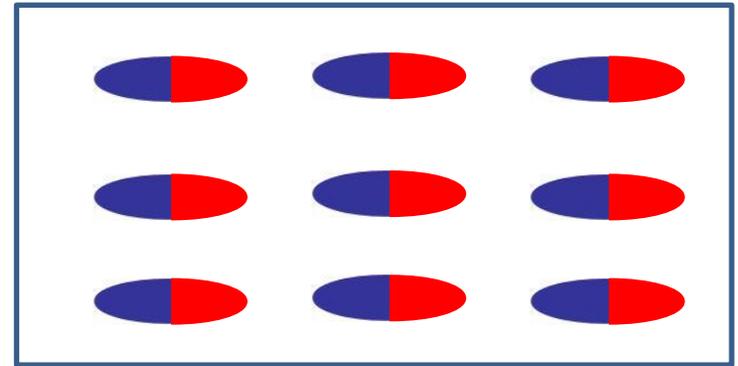


METAL



$$E=0$$

DIELECTRIC



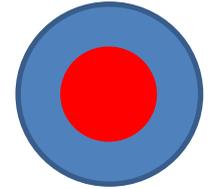
$$E_d$$

$$\overline{E}_d = \frac{\overline{E}_0}{\epsilon}$$

Screening mechanisms

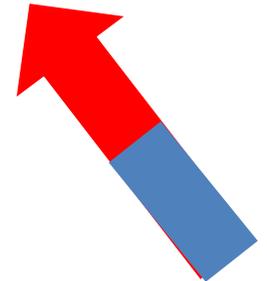
Electronic Polarizability
(Electron Cloud Distortion)

$$10^{15} \text{ s}^{-1}$$



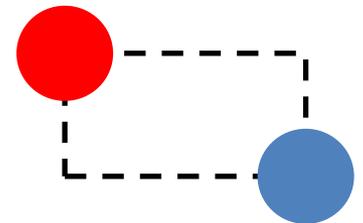
Dipole Re Orientation
(Langevin Mechanism)

$$10^8 - 10^{10} \text{ s}^{-1}$$

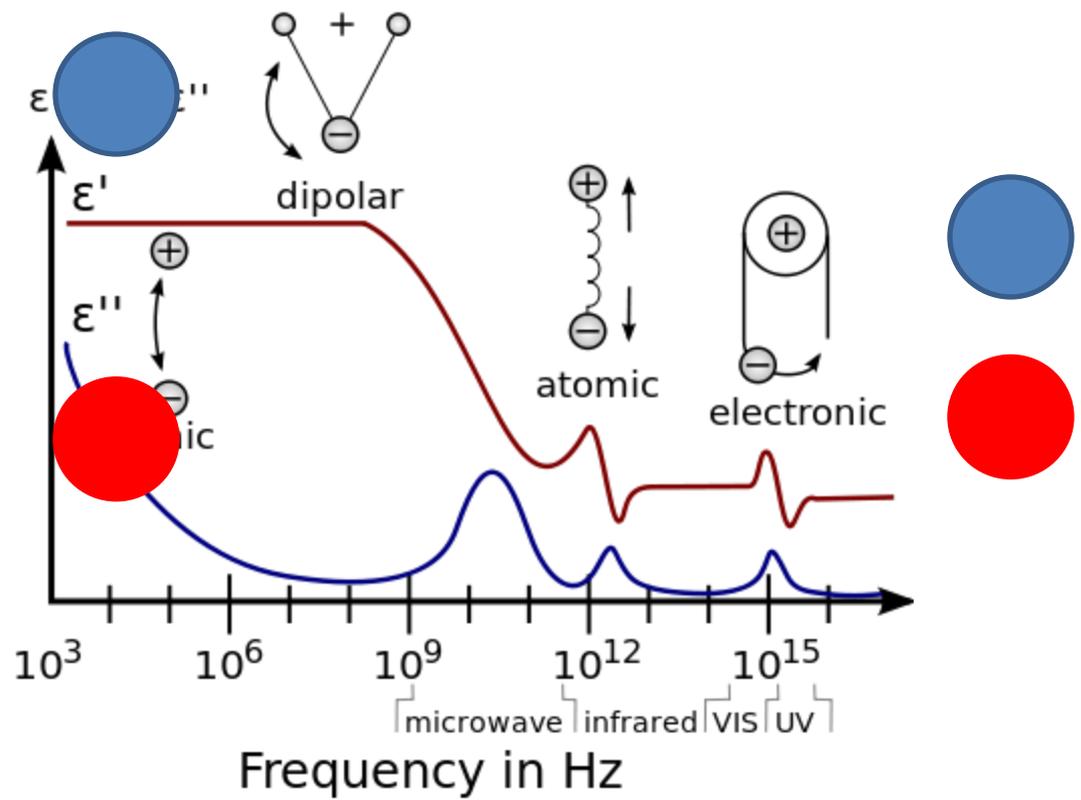


Ions Displacement
(Optical Phonons)

$$10^{10} - 10^0 \text{ s}^{-1}$$



Screening mechanisms

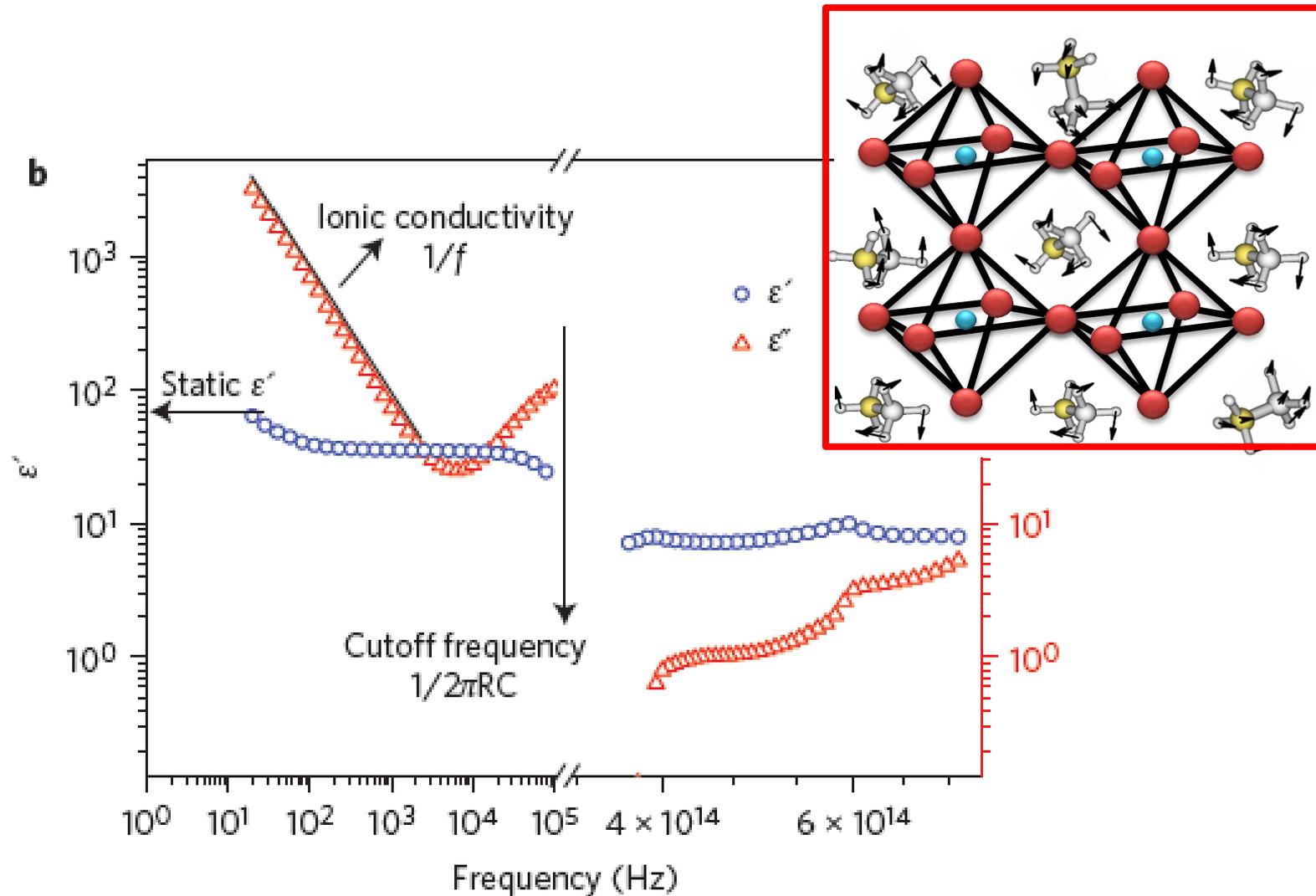


$$\prod_i \left(\frac{\omega_{Li}}{\omega_{Ti}} \right)^2 = \frac{\epsilon_0}{\epsilon_\infty}$$

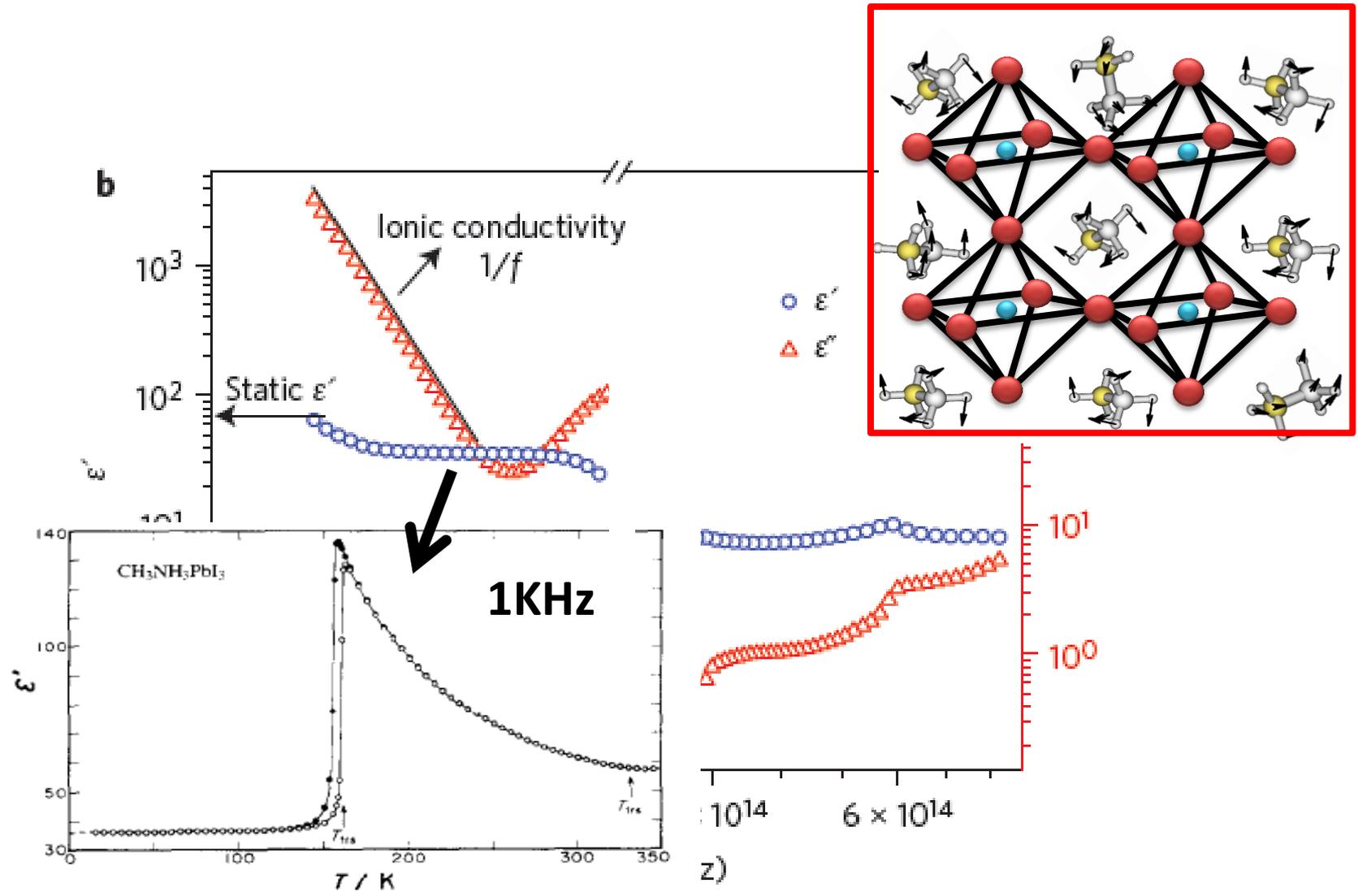
Dielectric constant of GaAs. Why it is so easy

- $\frac{\epsilon_0}{\epsilon_\infty} = 2$
- $\epsilon_0(T) = 12.4 + 0.00012 * T$
- $\omega_{LO} = 36\text{meV}$ $\omega_{TO} = 38\text{meV}$

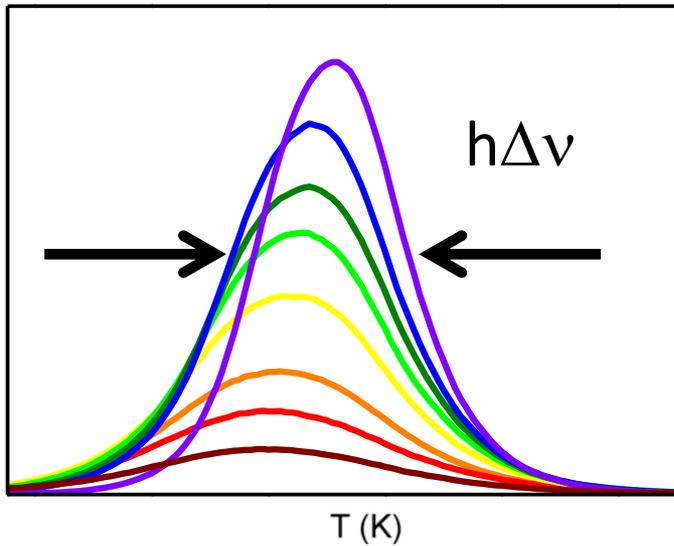
Dielectric constants of CH3NH3PbI3, real and imaginary parts



Dielectric constants of $\text{CH}_3\text{NH}_3\text{PbI}_3$, real and imaginary parts



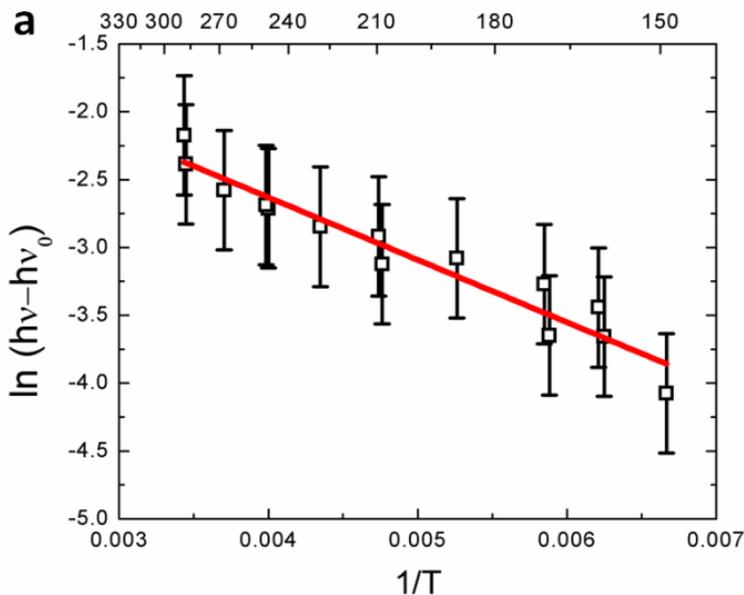
(I) Direct Measurement of Exciton Binding Energy in $\text{CH}_3\text{NH}_3\text{PbI}_3$



Exciton Binding Energy

$$\Delta\nu = k_1 + \nu \exp\left(-\frac{E_b}{k_B T}\right)$$

E_b (upper limit) = 50meV



Limitations:

→ It is assumed that exciton-phonon interaction induces only exciton dissociation

→ though in a limited range – it assumes the exciton binding energy constant in T

(I) Direct Measurement of Exciton Binding Energy in $\text{CH}_3\text{NH}_3\text{PbI}_3$

$$\Delta\nu = \frac{1}{\pi T_2}$$

$$\frac{1}{T_2} = \frac{1}{2T_1} + \gamma$$

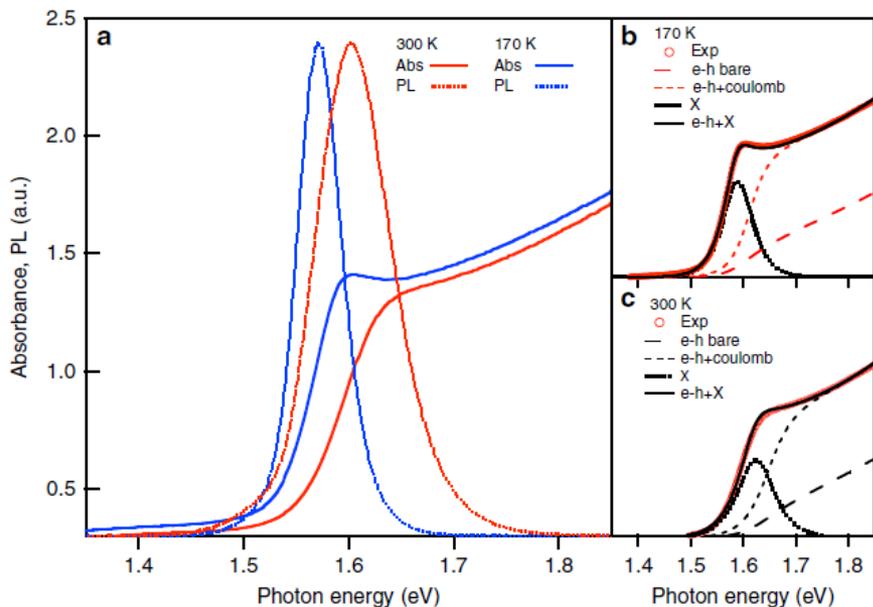
$$\frac{1}{T_1} = k_0 + k_T$$

$$k_T = \nu_T e^{-E_B/k_B T}$$

(II) Direct Measurement of Exciton Binding Energy in $\text{CH}_3\text{NH}_3\text{PbI}_3$

Numerical modelling of band-edge absorption by using Elliot's theory of Wannier excitons

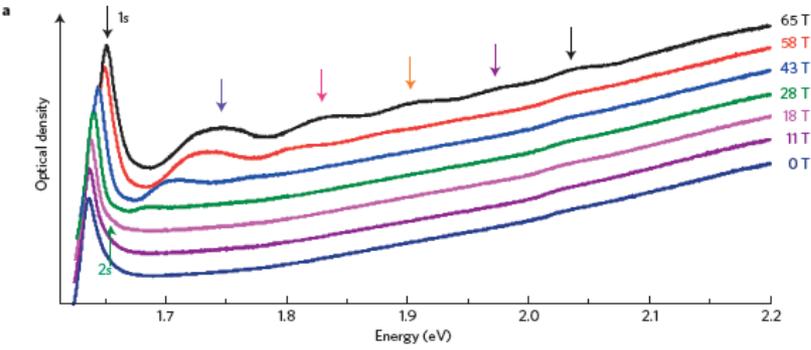
$$\alpha(\hbar\omega) \propto \mu_{cv}^2 \frac{\hbar\omega}{E_b} \left[\sum_j \frac{4\pi E_b}{j^3} \cdot \text{sech}\left(\frac{\hbar\omega - E_g + E_b/j^2}{\Gamma}\right) + \int_{E_g}^{\infty} \text{sech}\left(\frac{\hbar\omega - \varepsilon}{\Gamma}\right) \cdot \frac{2\pi}{1 - e^{-2\pi\sqrt{E_b}/\varepsilon - E_g}} \cdot \frac{1}{1 - \frac{8\mu b}{\hbar^3}(\varepsilon - E_g)} d\varepsilon \right]$$



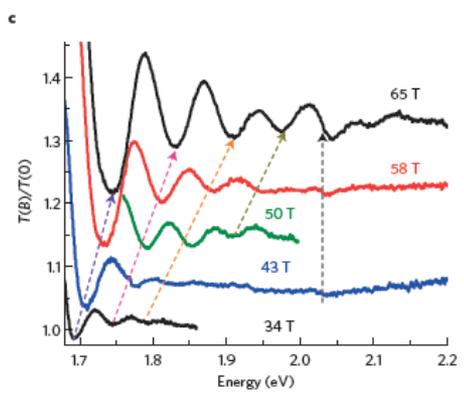
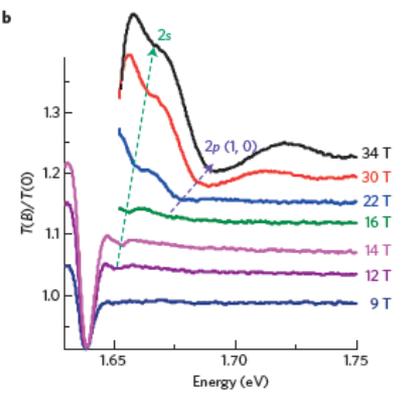
$$E_b = 25\text{meV}$$

Note: This simple formalism does not consider the frequency dependence of the exciton-phonon interaction

(III) Direct Measurement of Exciton Binding Energy in $\text{CH}_3\text{NH}_3\text{PbI}_3$



$$E(B) = E_g + (N + 1/2)\hbar\left(\frac{eB}{m^*}\right)$$



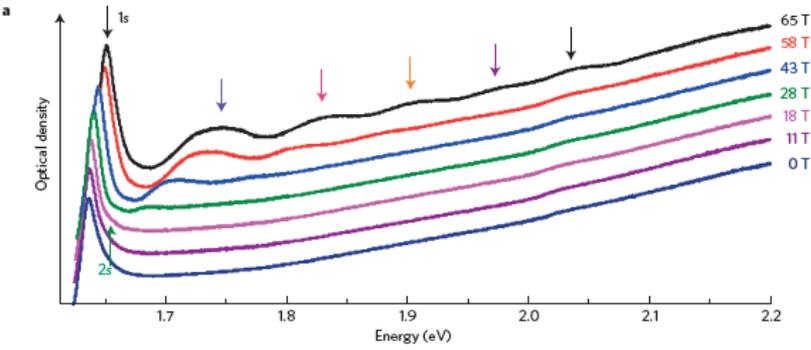
$$E_n = E_g - \frac{R}{n}$$

At 4K

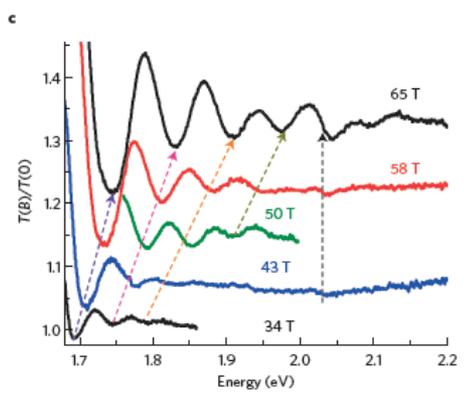
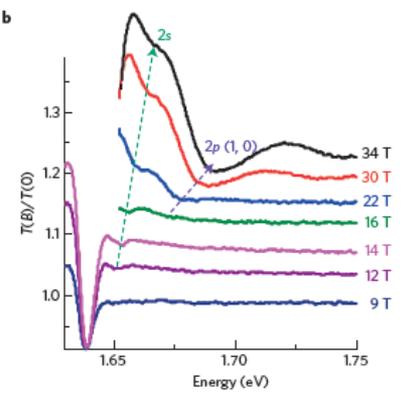
$$m^* = 0.1m ; \quad E_b = 16\text{meV}$$

$\epsilon \sim 9$

(III) Direct Measurement of Exciton Binding Energy in $\text{CH}_3\text{NH}_3\text{PbI}_3$



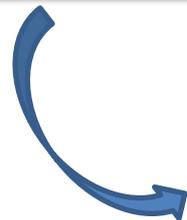
$$E(B) = E_g + (N + 1/2)\hbar\left(\frac{eB}{m^*}\right)$$



$$E_n = E_g - \frac{R}{n}$$

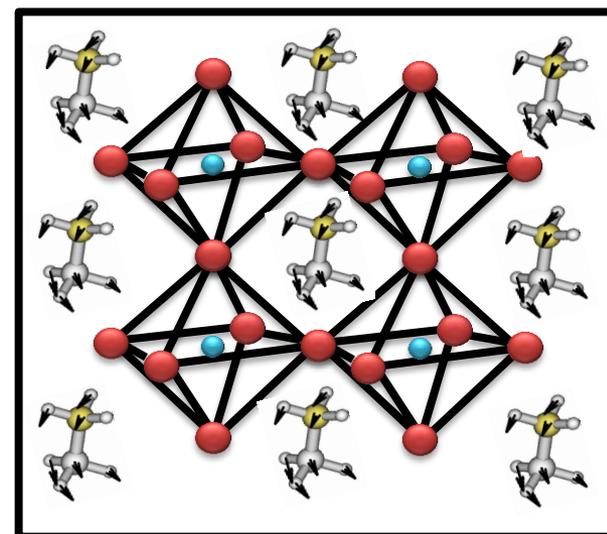
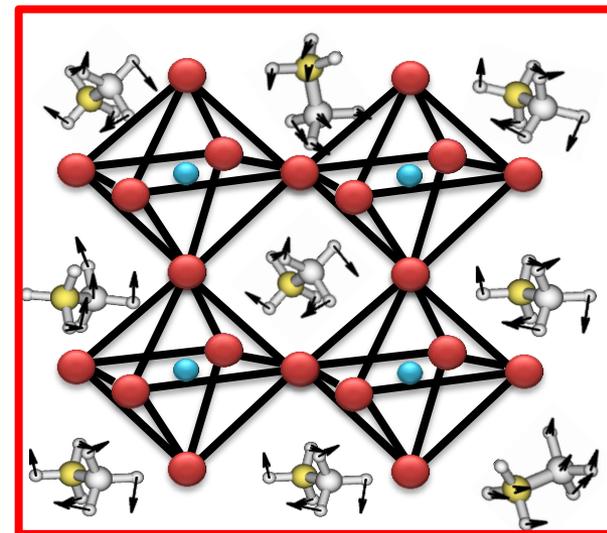
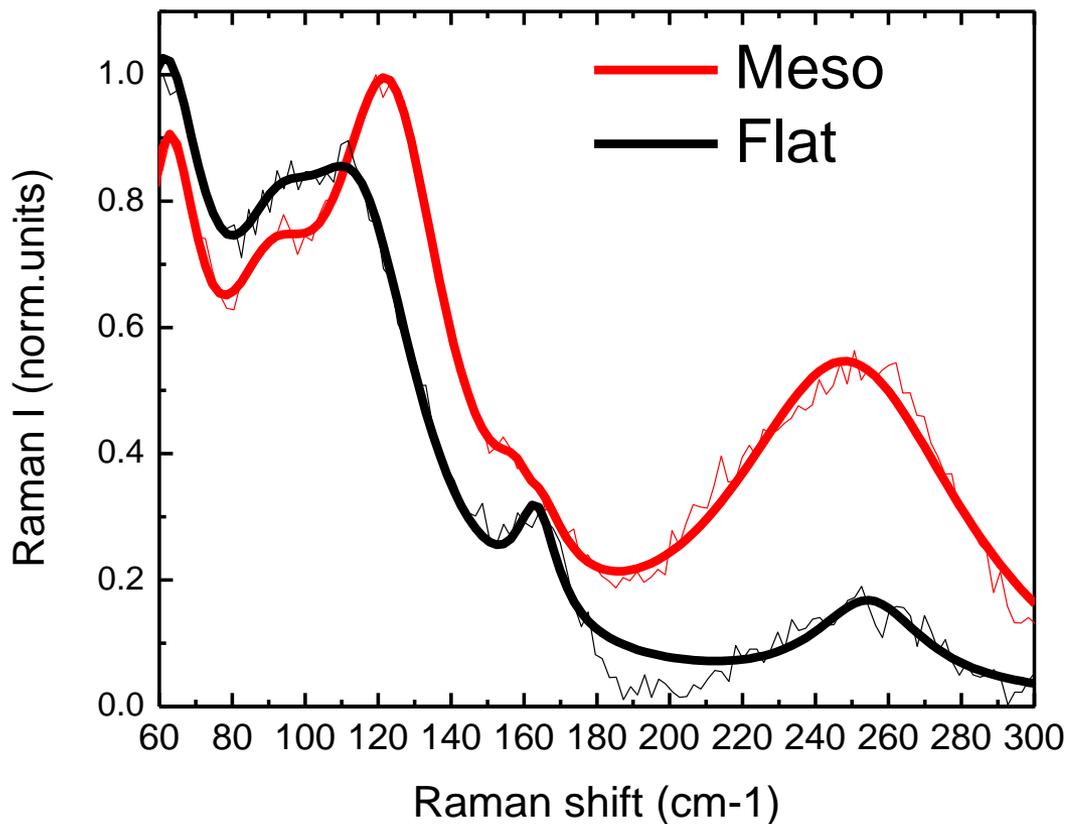
At 161K

$E_b \sim 10 \text{ meV}$



$\epsilon > 9$

Organic-Inorganic Interplay: Raman Spectroscopy as a probe



- Light Absorption
- **Charge Generation**
- Photo-carriers Transport

Exciton Vs Free Charges

at the Thermodynamic Equilibrium

Total excitation density

$$n = n_{FC} + n_{exc}$$

Excitons

Free charges

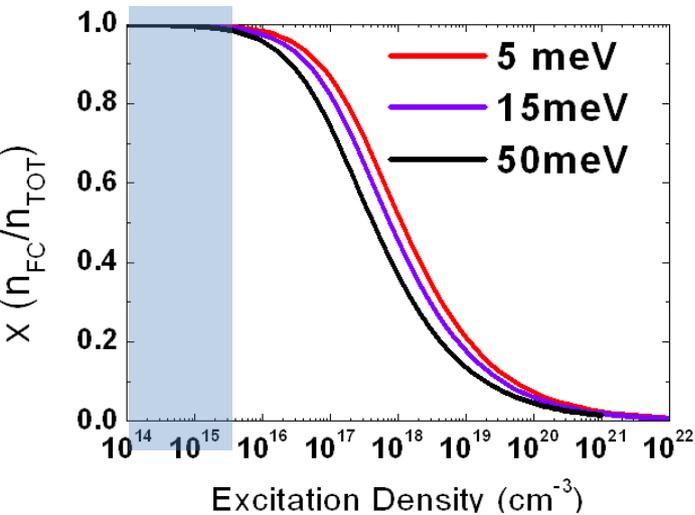
$$\frac{n_{FC}}{n_{exc}} = \left(\frac{2\pi\mu k_B T}{h^2} \right)^{3/2} e^{-\frac{E_b}{k_B T}}$$

$$x = \frac{n_{FC}}{n}$$

**Saha-Langmuir
equation**

Are there excitons around? MAPbI₃

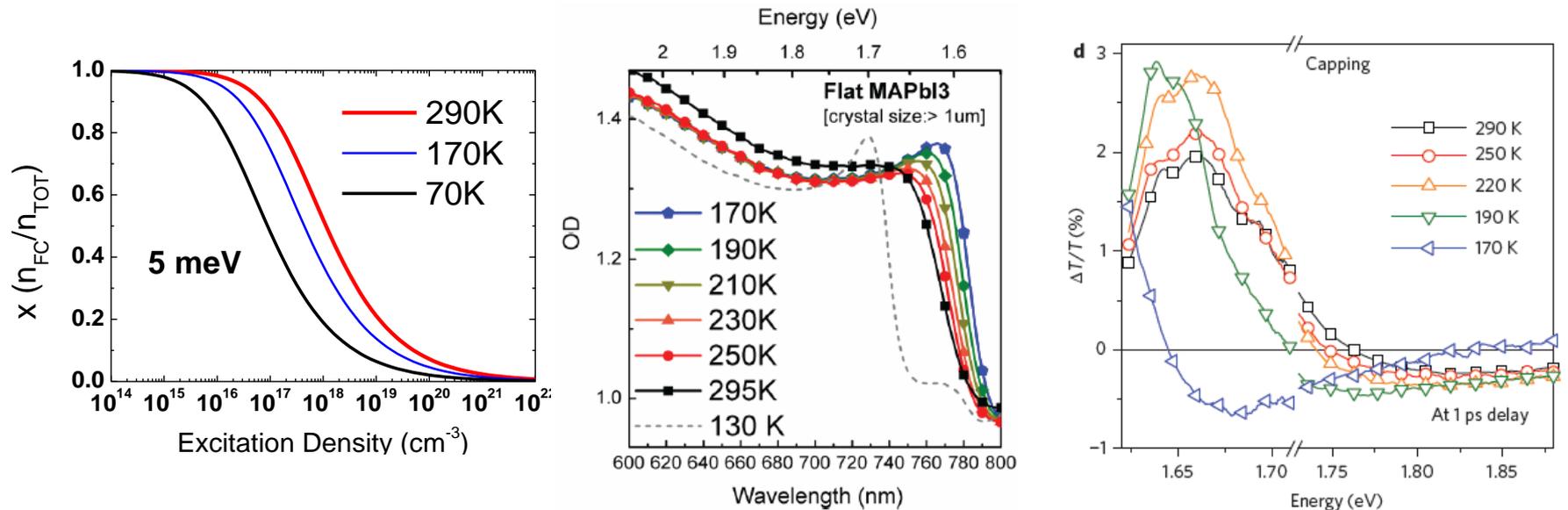
- **Room Temperature**, in the typical PV regime $\eta_{ph} < 10^{16} \text{ cm}^{-3}$:
free carriers only



- THz conductivity spectra are Drude-like in accordance with the presence of free charge carriers. Wehrefenning et al, Adv Mater, 26, 1584, 2014, Milot et al, Adv Funct Mater, 2015 DOI: 10.1002/adfm.201502340,
- PL dynamics are dictated by bimolecular recombination processes. Yamada, Y J. Am. Chem. Soc. 2014, 136, 11610. Stranks, Phys. Rev. Appl. 2014, 2 034007.
- fs-TA spectra show band filling effect and Varnshi –shift. Kamat et al, Nature Photonics, 2014; Grancini&Kandada et al, Nature Photonics 2015

The deal for PV is:
 we exploit the presence of the exciton transition for light harvesting without paying in charge dissociation

- Low Temperature, Exciton population is detectable.



→ THz spectra probe localization effects as a consequence of exciton formation below 80K. Milot et al, Adv Funct Mater, 2015 DOI:

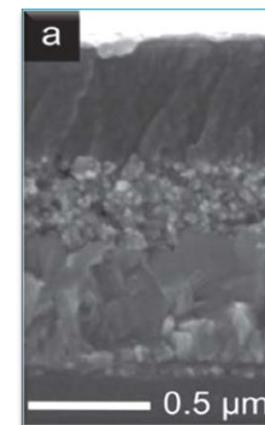
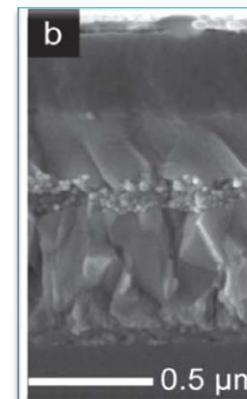
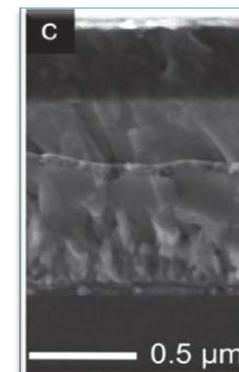
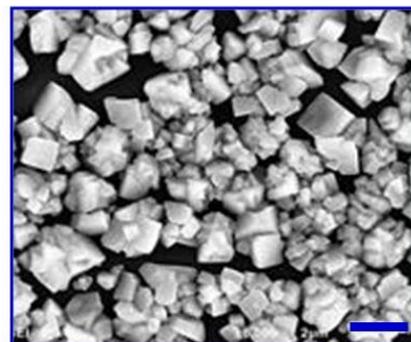
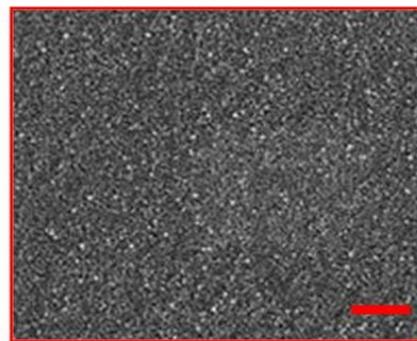
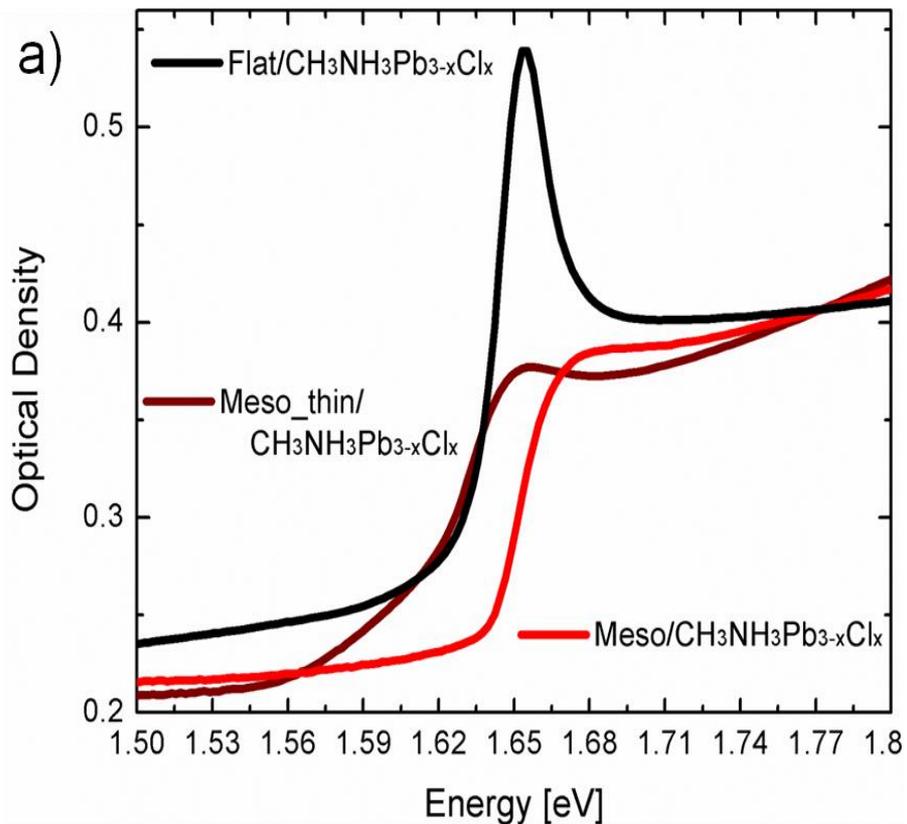
10.1002/adfm.201502340,

→ fs-TA spectra show a modulation of the photo-bleach as a result of exciton-exciton interaction. Grancini&Kandada et al, Nature Photonics 2015

WARNING: The Exciton binding energy increases (the dielectric constant decreases) when cooling down! → Miyata et al, Nature Physics 11, 582–587 (2015)

Local order/ microstructure

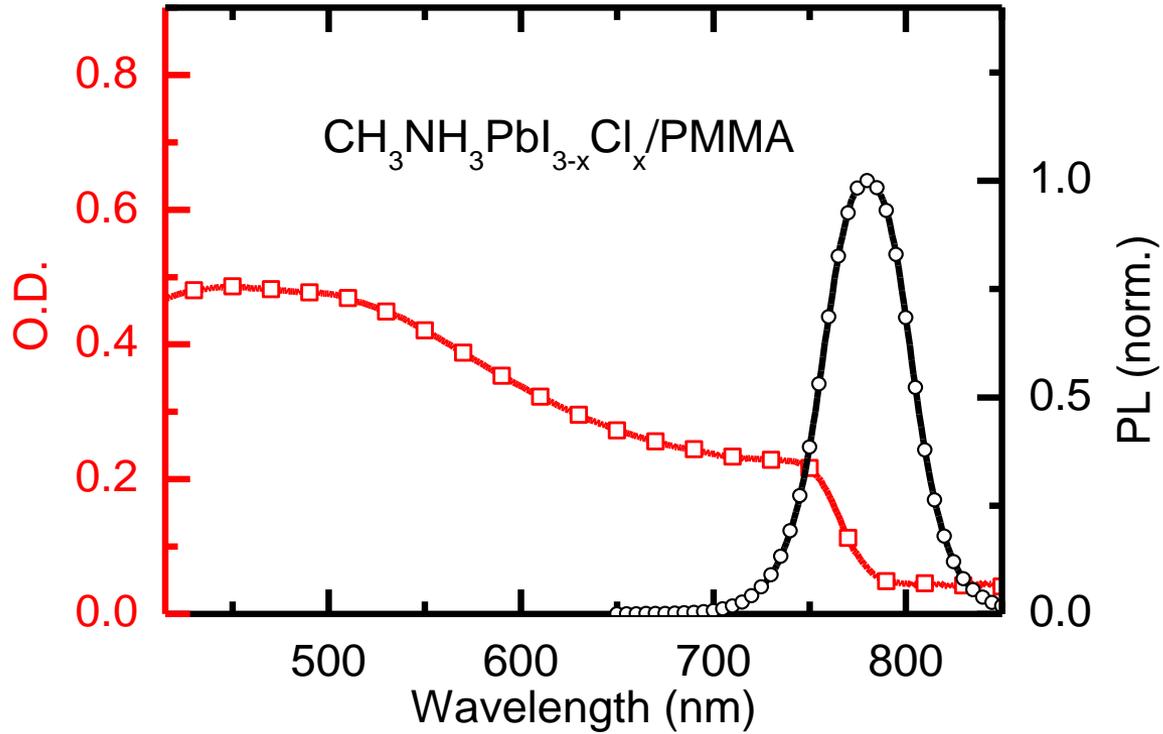
MAPbI₃



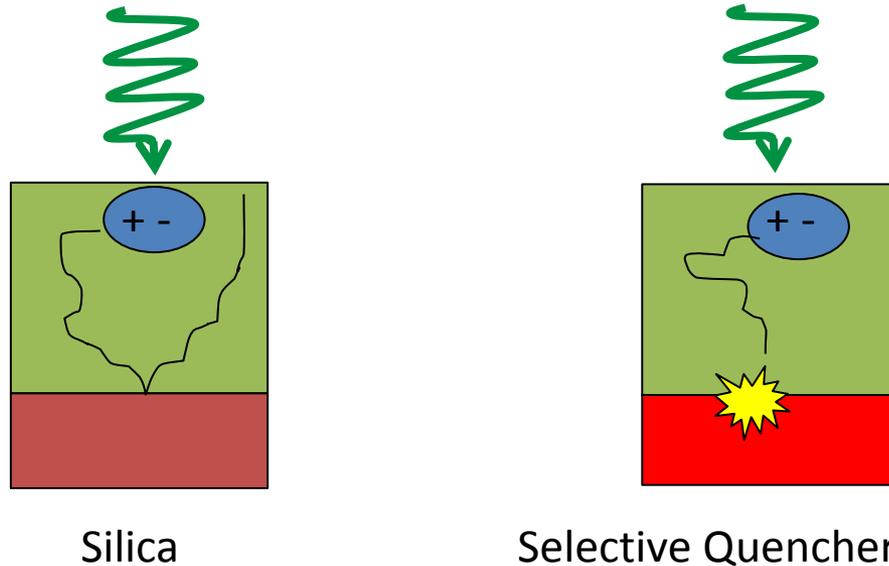
Designing the Device Architecture

- Light Absorption
- Charge Generation
- **Photo-carriers Transport**

Photo-carriers Diffusion Length



Electron-Hole Diffusion Lengths By Photoluminescence Quenching



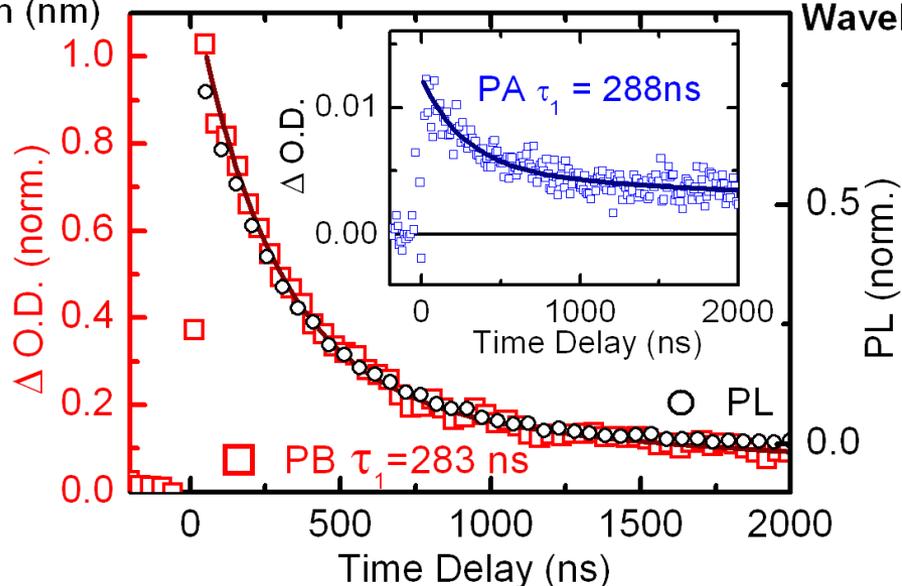
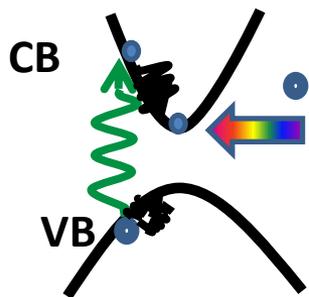
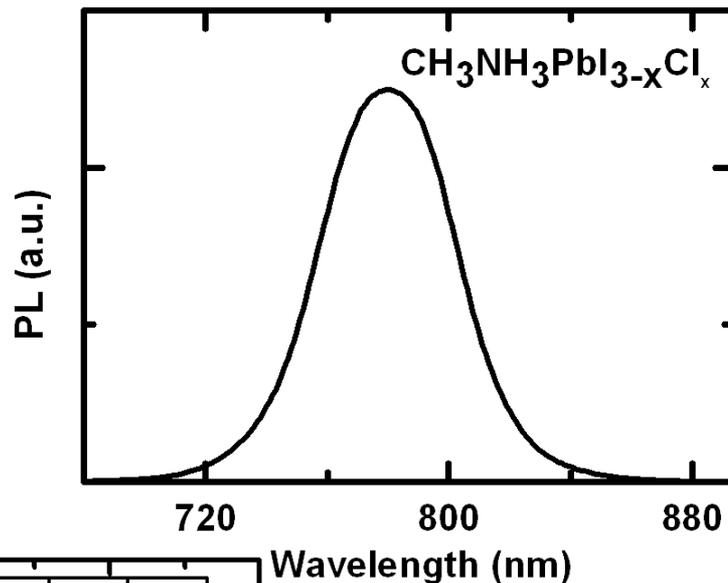
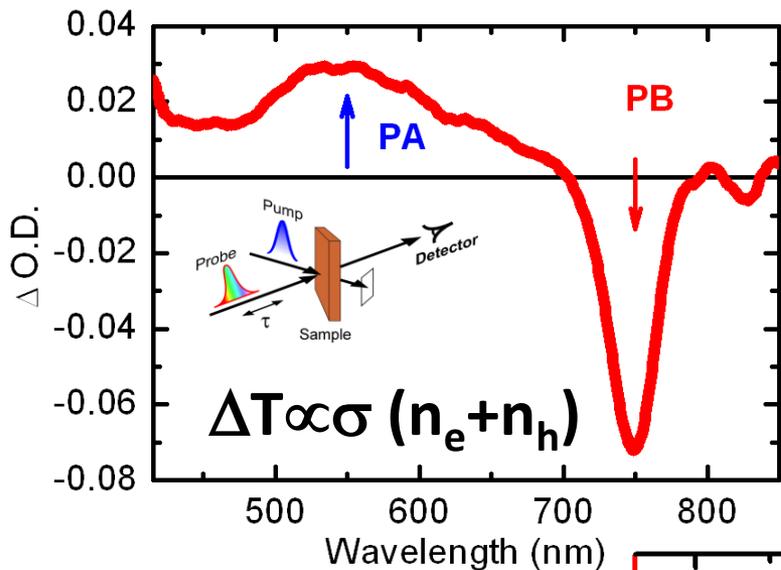
$$\frac{\partial n(z, t)}{\partial t} = D \frac{\partial^2 n(z, t)}{\partial z^2} - k(t)n(z, t)$$

Diffusion constant

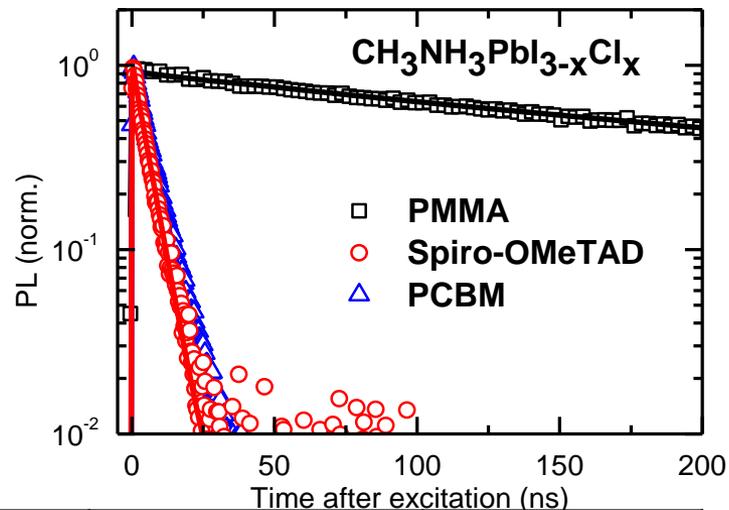
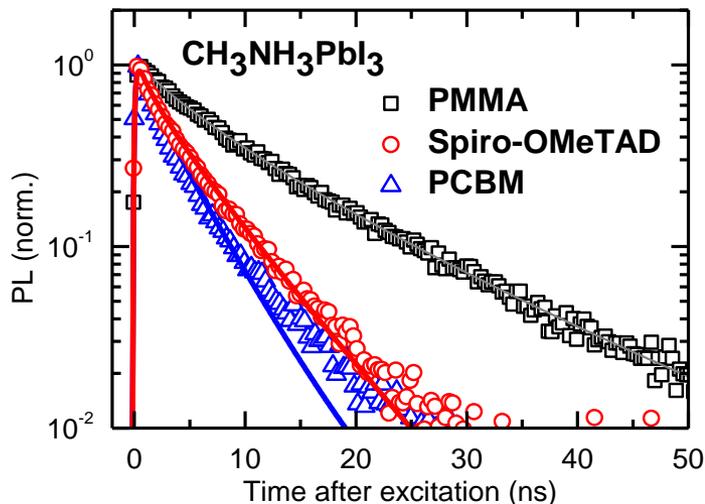
Natural decay rate
 (no quencher)

Electron-Hole Diffusion Lengths

By Photoluminescence Quenching



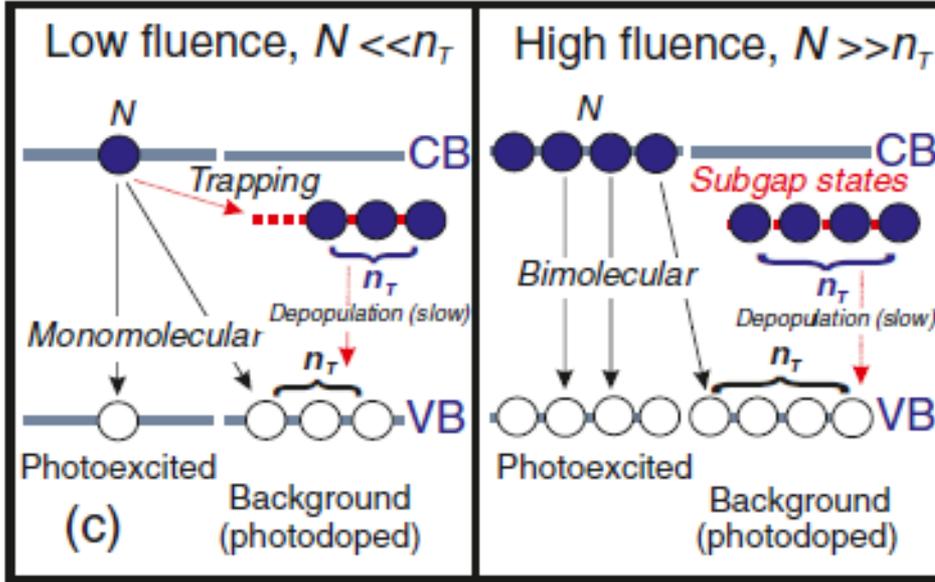
Electron-Hole Diffusion Lengths By Photoluminescence Quenching



Perovskite	Species	D (cm ² s ⁻¹)	L _D (nm)
CH ₃ NH ₃ PbI _{3-x} Cl _x	Electrons	0.042 ± 0.016	1094 ± 210
	Holes	0.054 ± 0.022	1242 ± 250
CH ₃ NH ₃ PbI ₃	Electrons	0.017 ± 0.009	117 ± 29
	Holes	0.012 ± 0.005	96 ± 22

Time-resolved Photoluminescence

Stranks et al



$$\frac{dn}{dt} = -An - B_{rad}n^2$$

$$\left(\frac{1}{\tau_{PL}}\right) = k_{PL} = k_r + k_{nr}$$

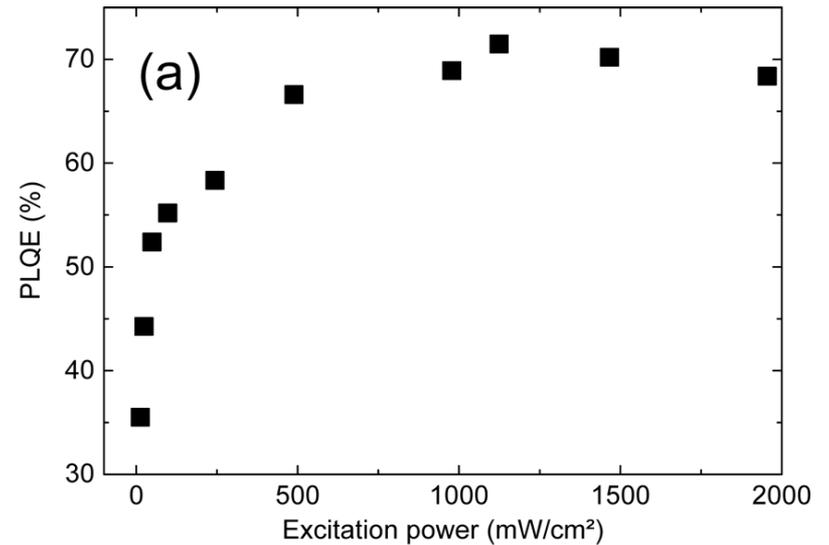
→ Yamada, Y J. Am. Chem. Soc. 2014, 136, 11610.

→ Stranks, Phys. Rev. Appl. 2014, 2 034007.

→ Saba, M.; Nat. Commun. 2014, 5 No. 5049.

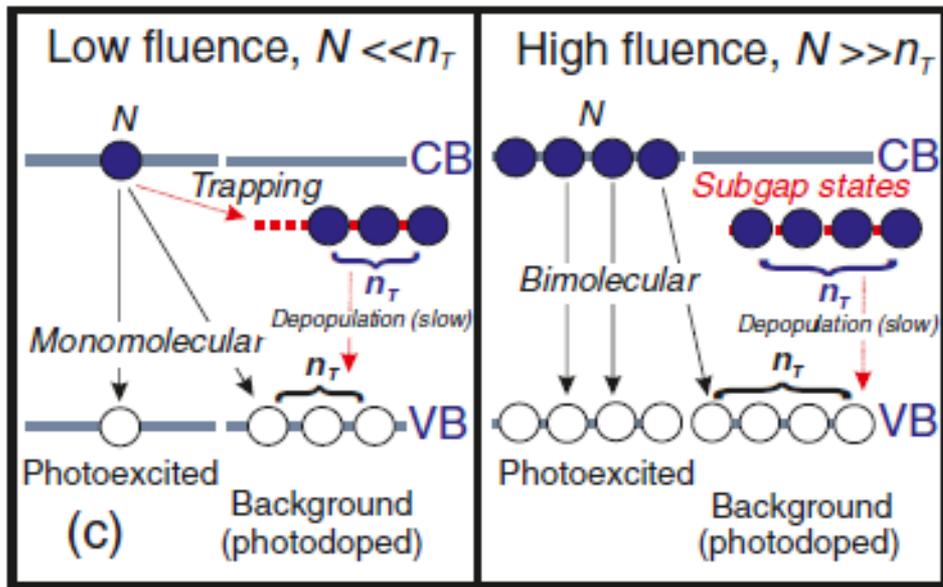
→ D’Innocenzo, J. Am. Chem. Soc. 2014, 136 (51), pp 17730–1773

→ Deschler, J. Phys. Chem. Lett. 2014, 5, 1421.



Deschler, et al

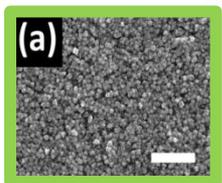
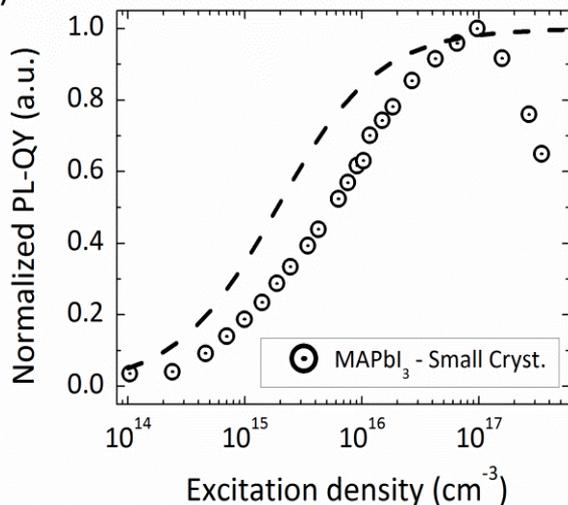
Time-resolved Photoluminescence



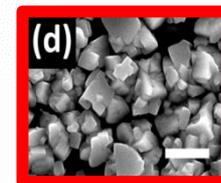
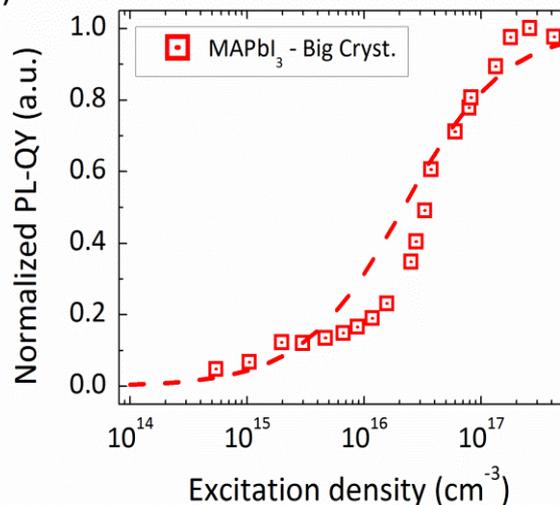
$$\frac{dn}{dt} = -An - B_{rad}n^2$$

$$\left(\frac{1}{\tau_{PL}}\right) = k_{PL} = k_r + k_{nr}$$

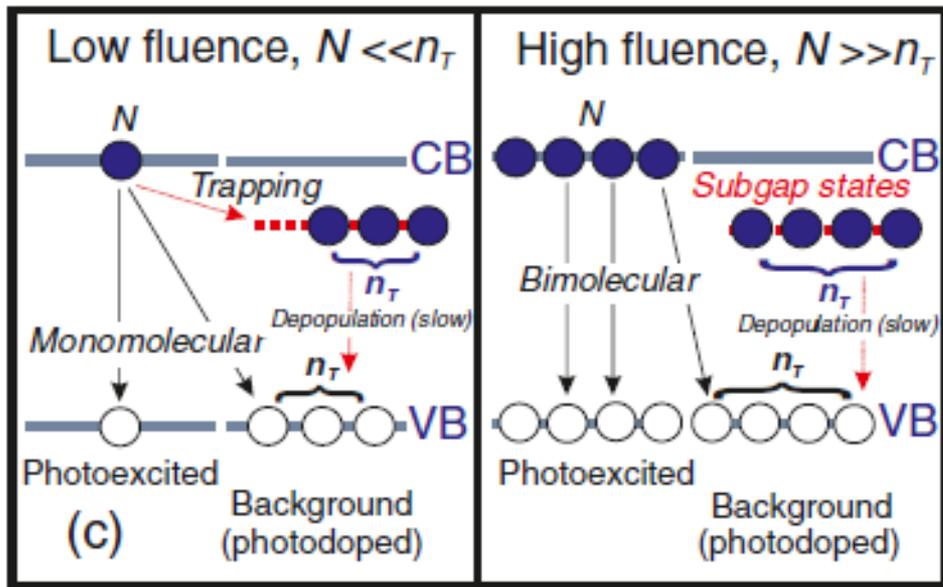
(a)



(b)

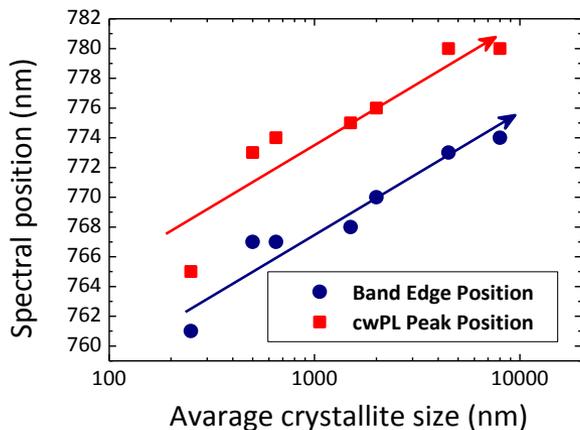
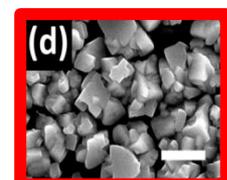
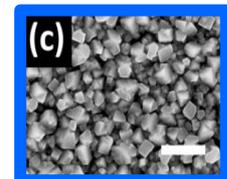
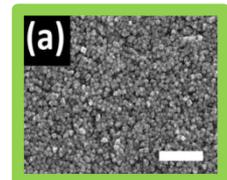


Time-resolved Photoluminescence



$$\frac{dn}{dt} = -An - B_{rad}n^2$$

$$\left(\frac{1}{\tau_{PL}}\right) = k_{PL} = k_r + k_{nr}$$



$$R_{rad}(E_G) = \int_{E_G}^{\infty} \rho_{ph}(\varepsilon) \alpha(\varepsilon) v_{ph}(\varepsilon) d\varepsilon$$

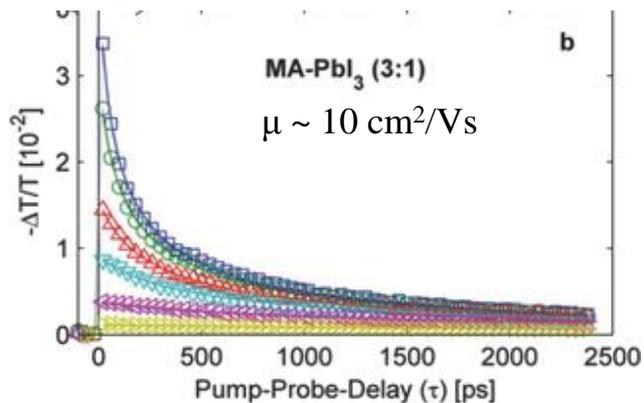
$$n_i(E_G) = \int_{E_{CBB}}^{\infty} \rho(\varepsilon) \frac{1}{1 + e^{(\varepsilon - \mu)/k_B T}} d\varepsilon$$

Measuring Charge-Transport in Perovskites

Terahertz/Microwave Spectroscopy

Simple sample preparation

Only informative on short length-scale

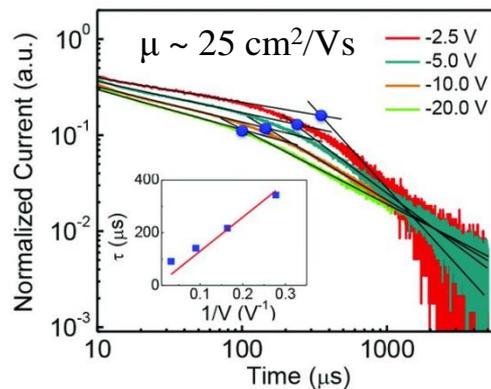


C. Wehrenfennig et al., Adv. Mat. (2013)

Time-of-flight

Relevant over longer length-scale

Time-scales difficult to measure in thin-film

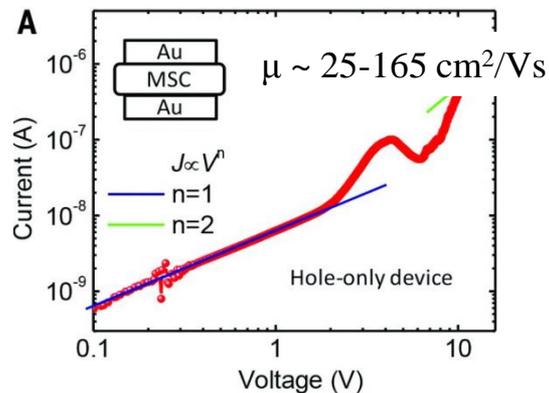


Q. Dong et al., Science (2015)

Space-charge limited current

Relevant to optoelectronic devices

Needs highly-selective non-limiting contacts

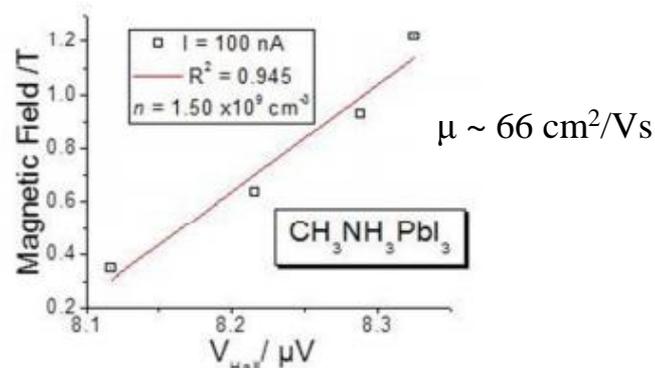


Q. Dong et al., Science (2015)

Hall-effect

Simultaneously get free-carrier density

Like THz, only band mobility obtained



C. Stoumpos et al., Inorg. Chem. (2013)

Take-home Message

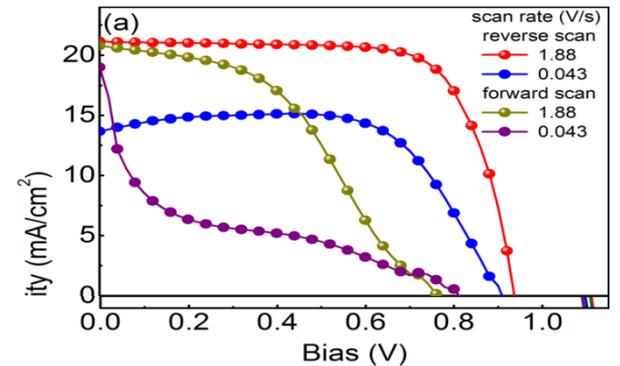
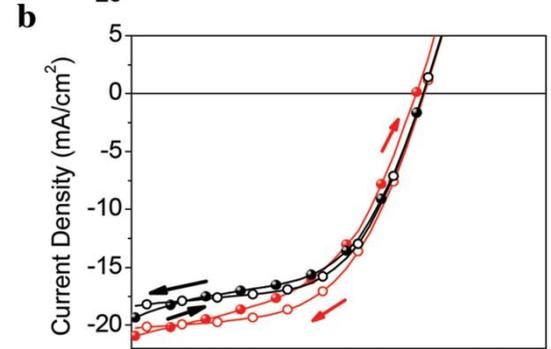
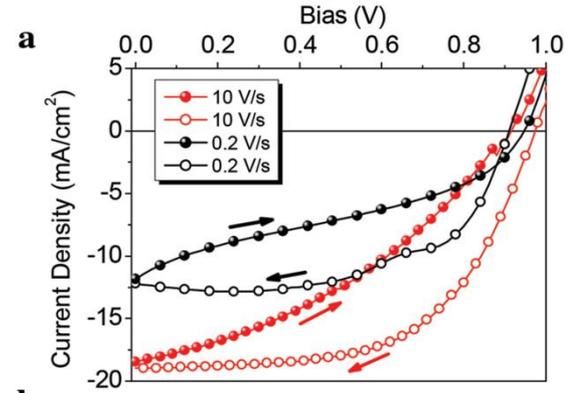
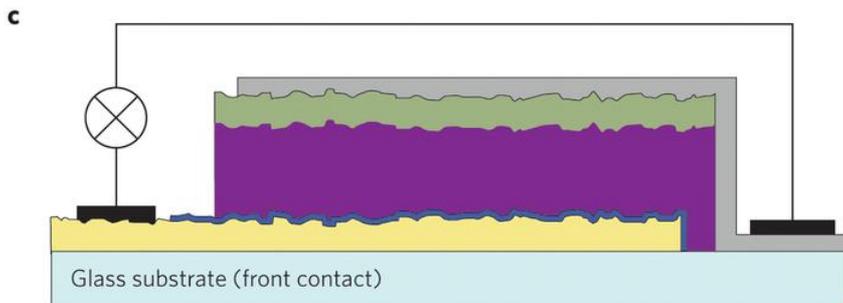
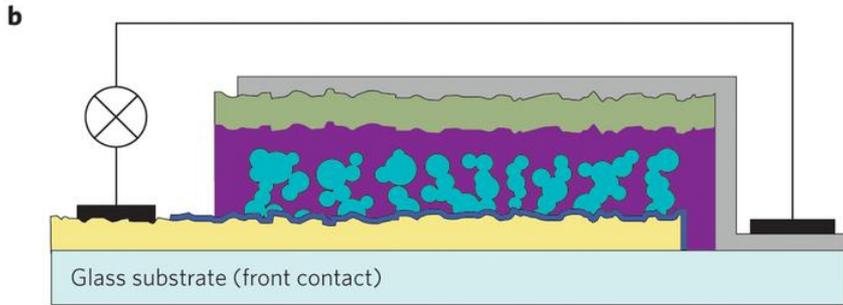
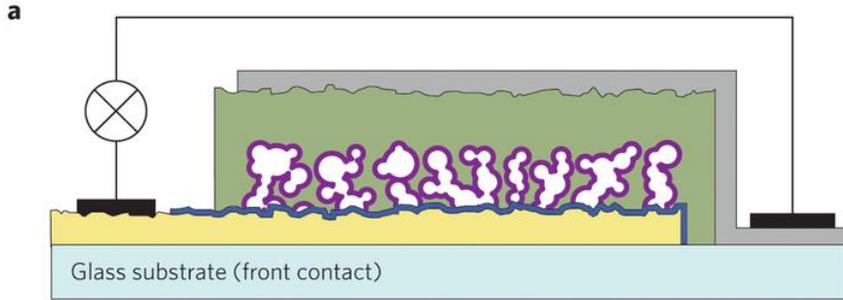
The room temperature structure of MAPbX₃ is a fluctuating structure where tilting and distortion of the octahedral networks and rotations and polarizability of the molecular dipole can strongly affect the optoelectronic properties of the semiconductor.

Open Questions

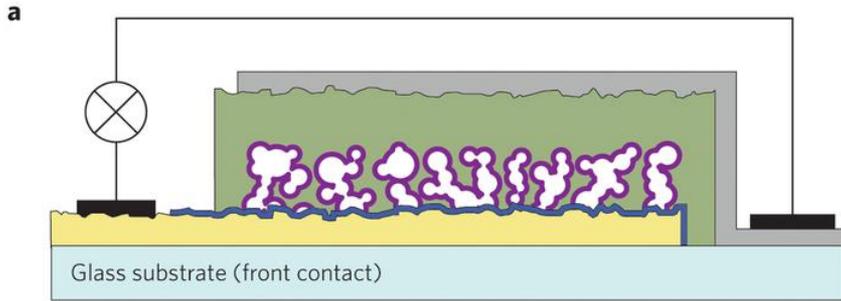
- Which is the secret of the low recombination rate
- Elucidation of the photo-carriers cooling
- Role of phonons
- Nature of carriers, localization vs delocalization
- Carriers transport mechanism

Vs Structural Properties

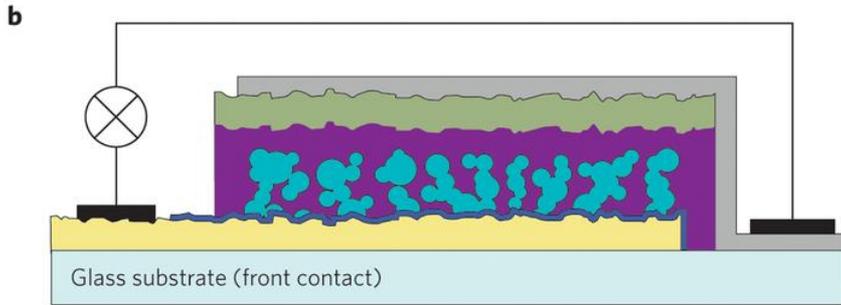
Technology



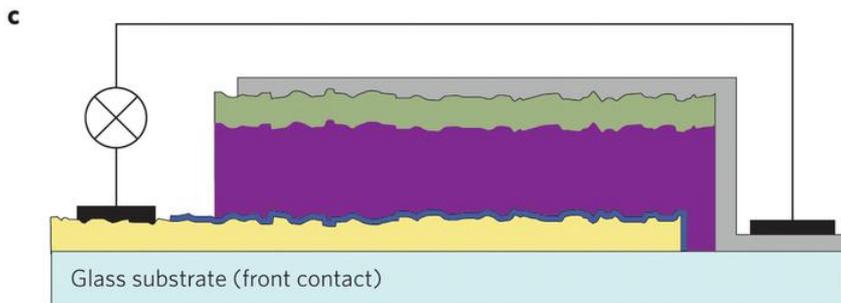
Technology



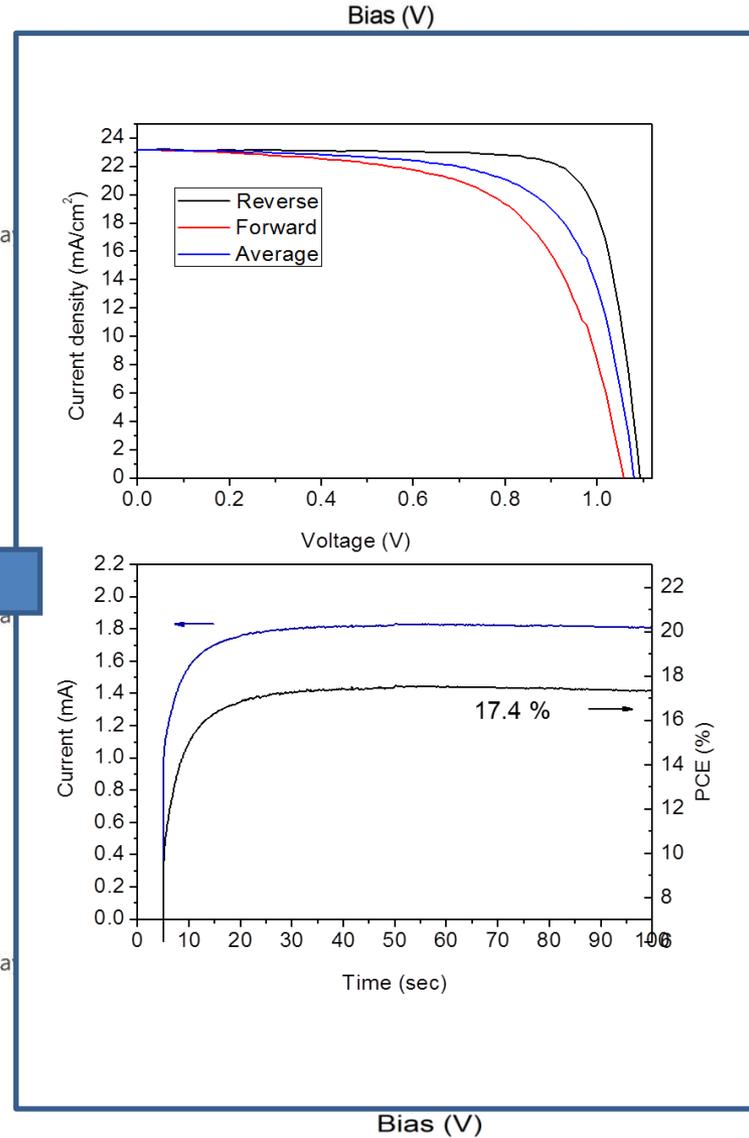
- Perovskite
- Al₂O₃
- HTM
- Compact TiO₂ la
- TCO
- Back contact



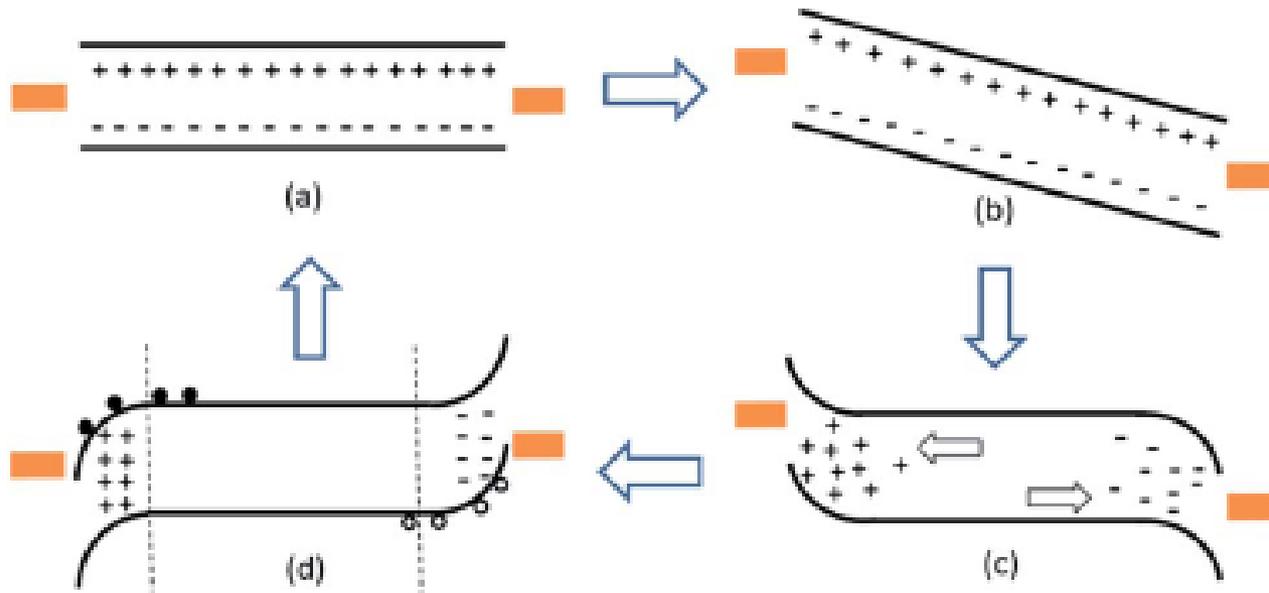
- Perovskite
- TiO₂
- Compact TiO₂ la
- TCO
- Back contact



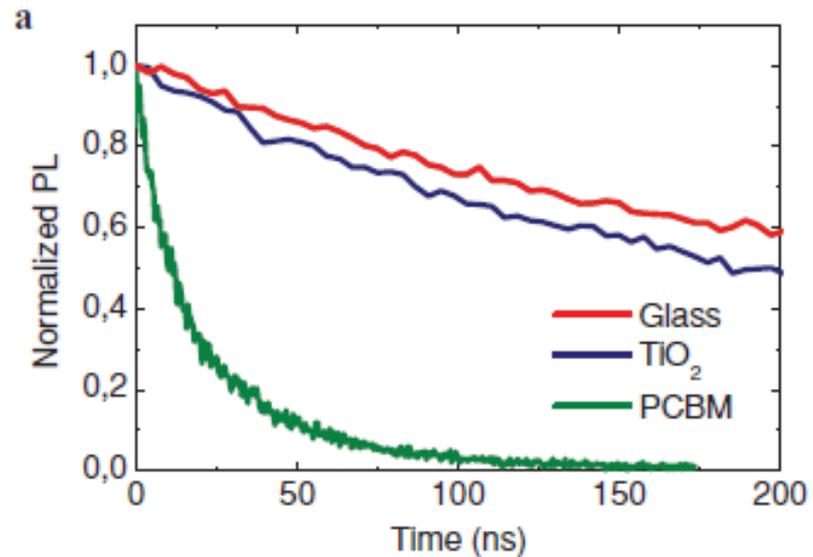
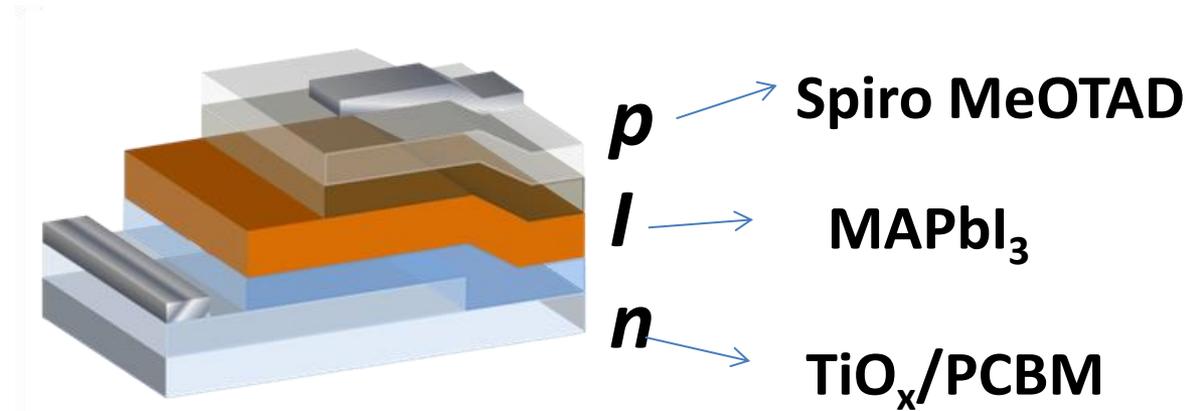
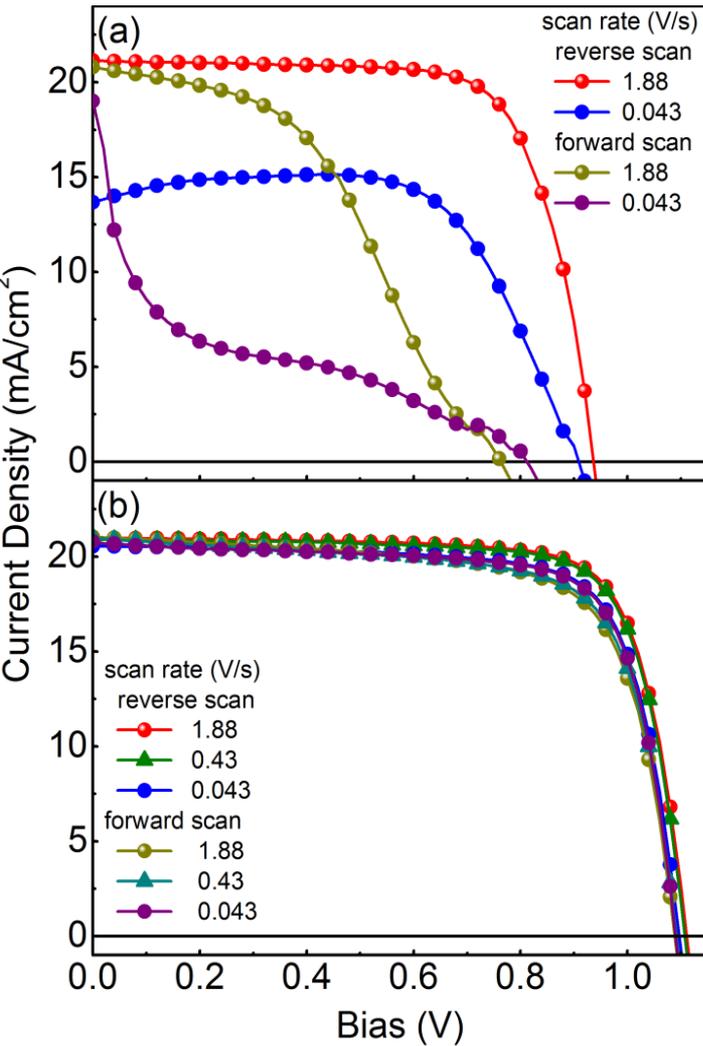
- Perovskite
- HTM
- Compact TiO₂ la
- TCO
- Back contact



Technology



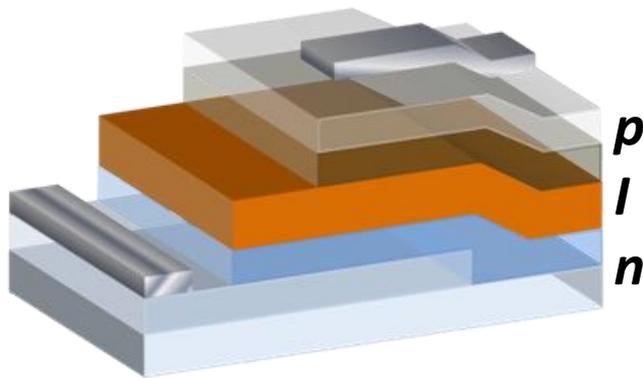
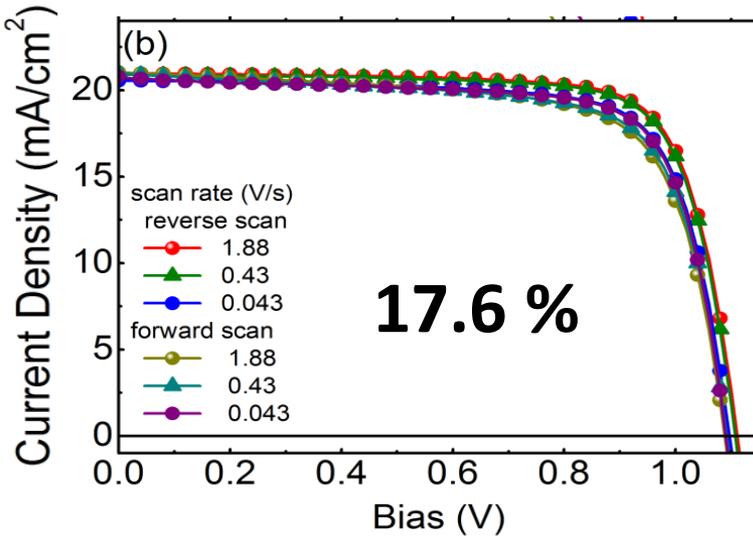
Perovskite PV at IIT



Perovskite PV at IIT

Technology Development

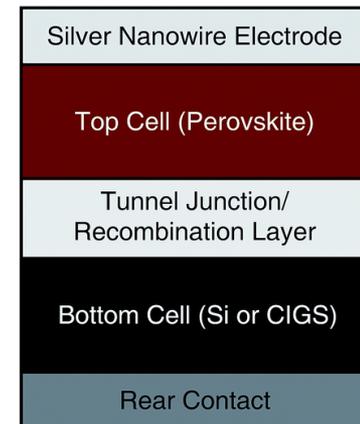
Fotovoltaico leggero e flessibile,
 a basso costo di produzione e
 energetico



Processi a bassa temperatura
 < 120 °C

Celle «TANDEM»

Aumento efficienza
 fotovoltaico tradizionale



Further Developments

- Interface Engineering
- Stability
- Toxicity
- ..